



Εκλάμψεις Ακτίνων γ Gamma-Ray Bursts

Μαρία Πετροπούλου

11 Ιουλίου 2026
Πάρκο Εθνικής Συμφιλίωσης

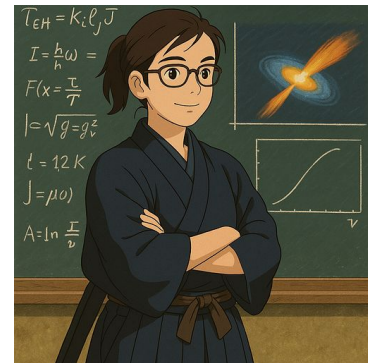


HELLENIC REPUBLIC
National and Kapodistrian
University of Athens

A few words about me

Main research interests

- Non-thermal radiative transfer
- Particle acceleration processes (magnetic reconnection)
- Astroparticle physics (high-energy neutrinos, cosmic rays)
- Modeling of high-energy astrophysical sources
 - Steady sources: Relativistic jets, cores of active galaxies
 - Transient sources: GRBs



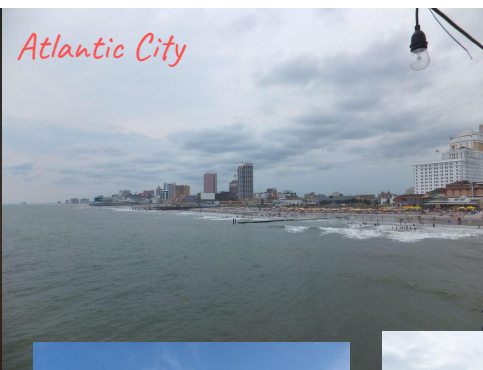
Indiana



Berlin



Atlantic City



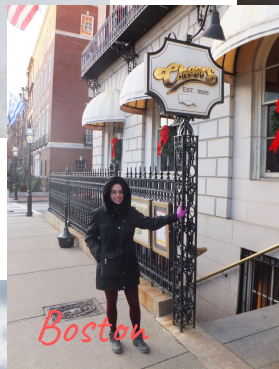
Hawai'i



Washington D.C. -
"Reflecting Pool"



Boston



Paris



Indiana



Geneva

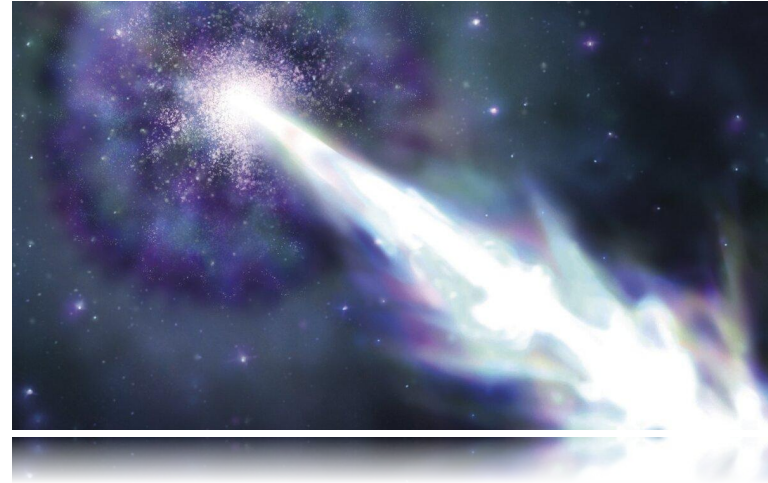


Strasbourg



Lecture plan

- Part 1: Introduction to Gamma-Ray Bursts (GRBs)
- Part 2: Introduction to GRB afterglows
- Part 3: Theory of GRB afterglows
- Part 4: Demonstration of *AfterglowPy*

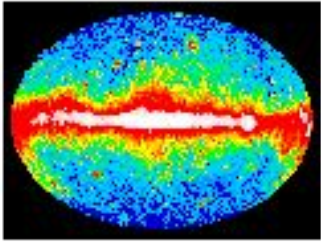


Part 1

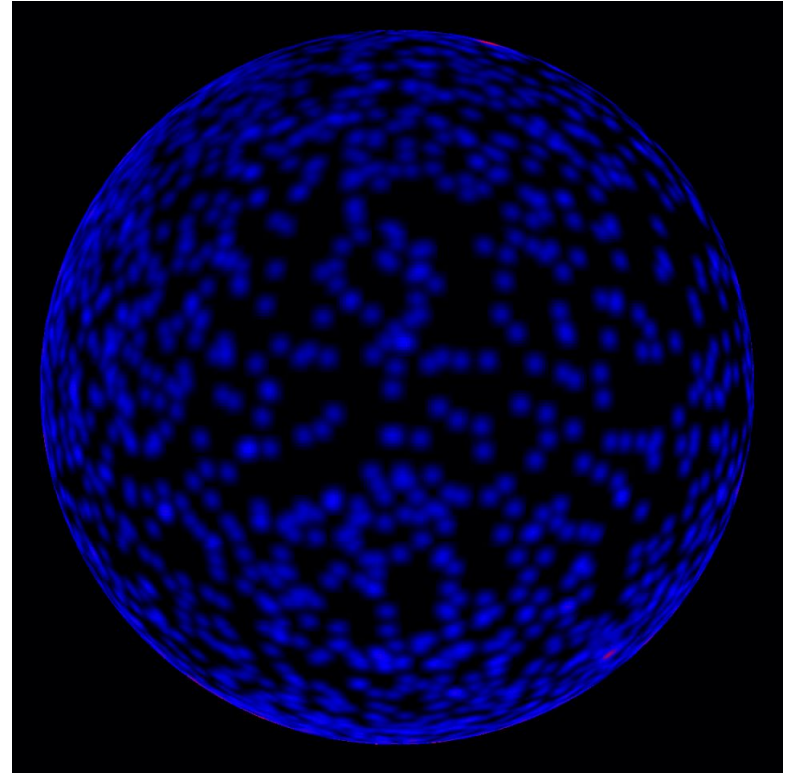
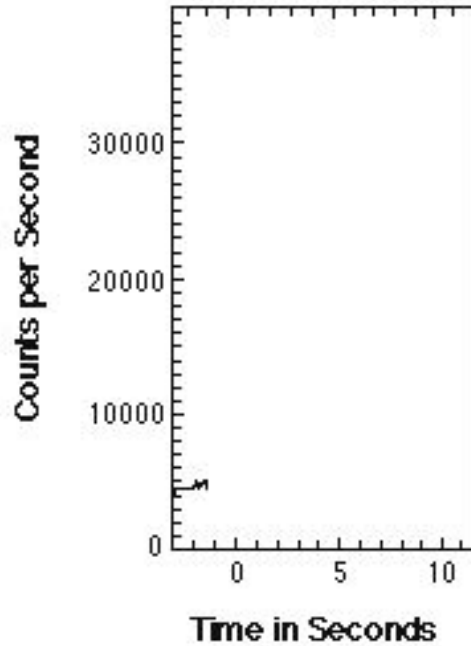


Introduction to GRBs

What are Gamma-Ray Bursts?



Credit: BATSE/CGRO

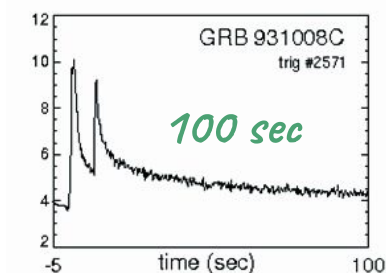
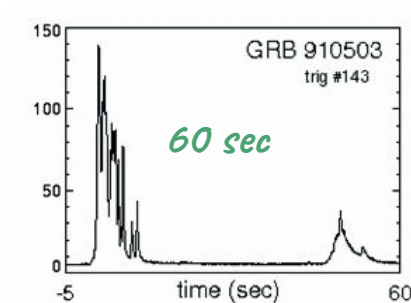
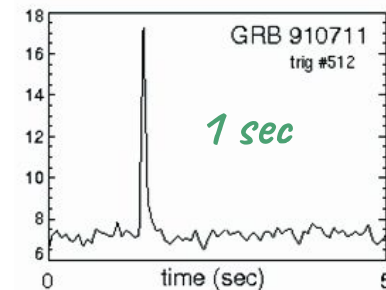
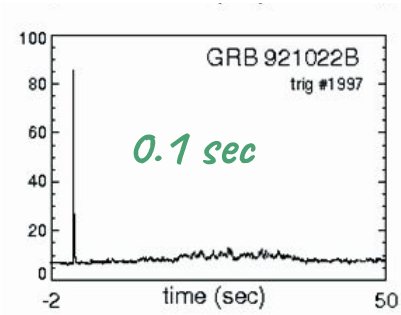


Credit: NASA/DOE/Fermi LAT Collaboration

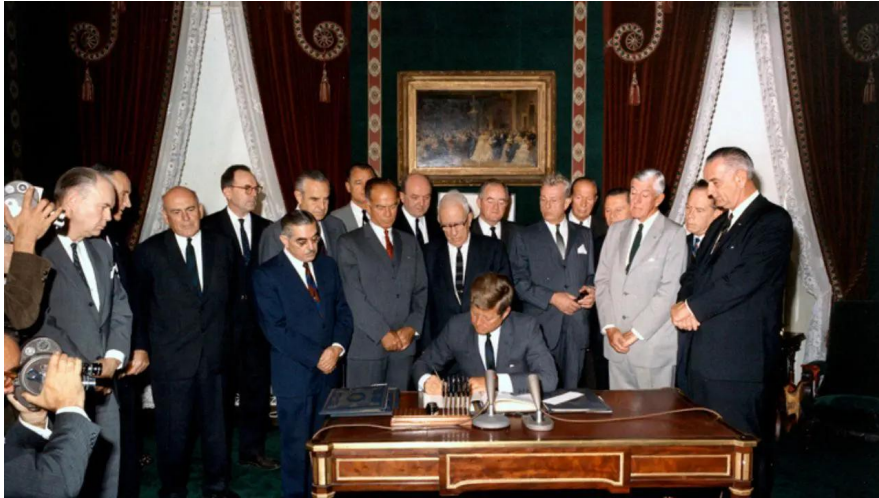
What are Gamma-Ray Bursts?

- Intense flashes of γ -ray radiation
- Short durations: ~ 0.1 s to 100 s
- Variability timescales:
 $\Delta t_{\text{var}} \sim \text{ms to } 1\text{s}$
- Causality argument*:
 $R < c \Delta t_{\text{var}} \sim (3 \times 10^7 - 10^{10}) \text{ cm}$

*ignoring relativistic effects



A random discovery

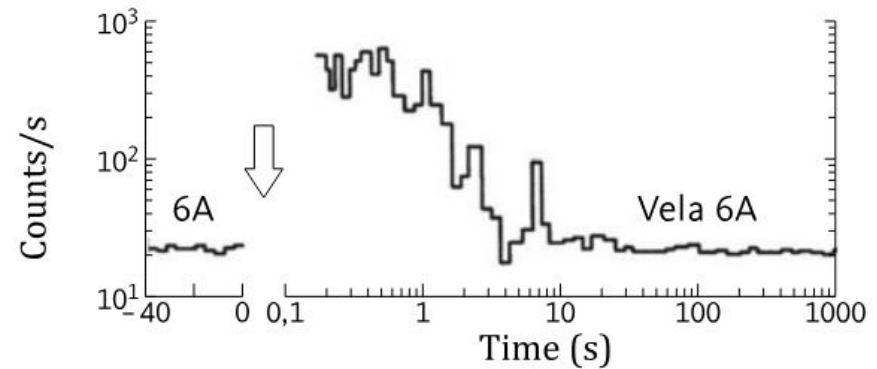


Partial Nuclear Test Ban Treaty, 1963

(Image Credit: The John F. Kennedy Presidential Library and Museum, Boston)



The first γ -ray flash (1967)



[Klebesadel, Strong, Olson, 1973, ApJ](#)

Cosmic Fireballs

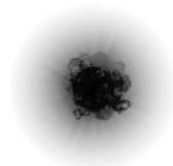
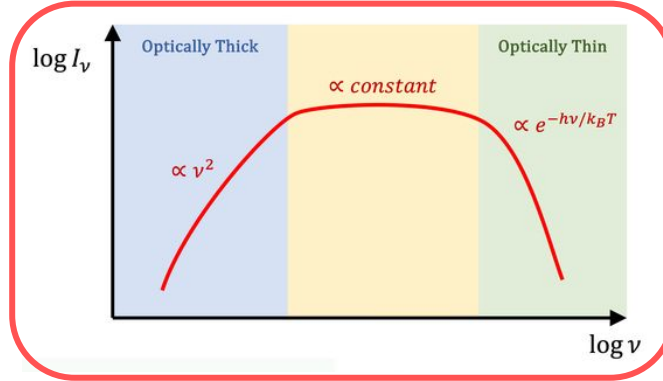
G. Cavallo[★] and M. J. Rees *Institute of Astronomy, Madingley Road,
Cambridge*

Received 1977 September 30

Summary. If a large amount of energy is suddenly converted into a concentrated burst of (MeV) γ rays, the prolific creation of electron–positron pairs will inhibit the escape of photons until they have been degraded below the pair-production threshold. This sets general constraints on the possible luminosities of rapidly varying γ -ray sources and suggests why the observed γ -ray bursts have an approximately standardized and ‘soft’ spectrum.



Cosmic Fireballs



The γ -ray fireball: e^-e^+p plasma and photons

Key physical processes:

1. Creation of e^+e^- pairs:
 $\gamma + \gamma \rightarrow e^+ + e^-$, $p + \gamma \rightarrow p + e^+ + e^-$

2. Creation of γ -ray photons:
 Bremsstrahlung, $e^+ + e^- \rightarrow \gamma + \gamma$

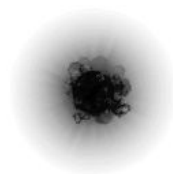
3. Compton scattering:
 $e + \gamma \rightarrow e + \gamma$

- a. Energy threshold: $\varepsilon_1 \varepsilon_2 (1 - \cos\theta) \geq 2 (m_e c^2)^2 \rightarrow \varepsilon \sim 1 (m_e c^2)$
- b. Cross section: $\sigma_{\gamma\gamma} \sim \sigma_T / \varepsilon^2$
- c. Degradation of γ -ray photon energy

- a. Cross section: $\sigma_T = \frac{8\pi}{3} \left(\frac{e^2}{m_e c^2} \right)^2$

- b. Diffusion of photons when $\tau_T \gg 1$

Cosmic Fireballs



Fireball Mass: $M_i \sim n_i m_p R^3 \left(n_p = n_e = n_i \right)$

Fireball Energy: $E_f = 10^{38} \text{ erg} \left(\frac{D}{100 \text{ pc}} \right)^2 \left(\frac{\Phi_\gamma}{10^{-4} \text{ erg cm}^2} \right) = \eta M_i c^2$

It can be smaller or larger than 1

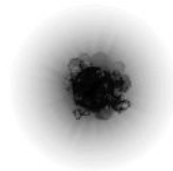
Fireball Luminosity: $L \sim \frac{E_f}{t_{\gamma, \text{diff}}} \sim \frac{c}{R} \frac{E_f}{\tau_T}$

Fireball adiabatic expansion: $t_{\text{exp}} \sim \frac{R}{u} \ll t_{\gamma, \text{diff}}, \text{ if } \tau_T \gg \frac{c}{u}$

$\varepsilon \sim R^{-1} \rightarrow E_f \sim R^{-1} \rightarrow u \nearrow$

$E_{\text{tot}} = \text{const} = E_{f, i} = E_{k, \infty} \Rightarrow u_\infty \sim \eta^{1/2} c$

Cosmic Fireballs



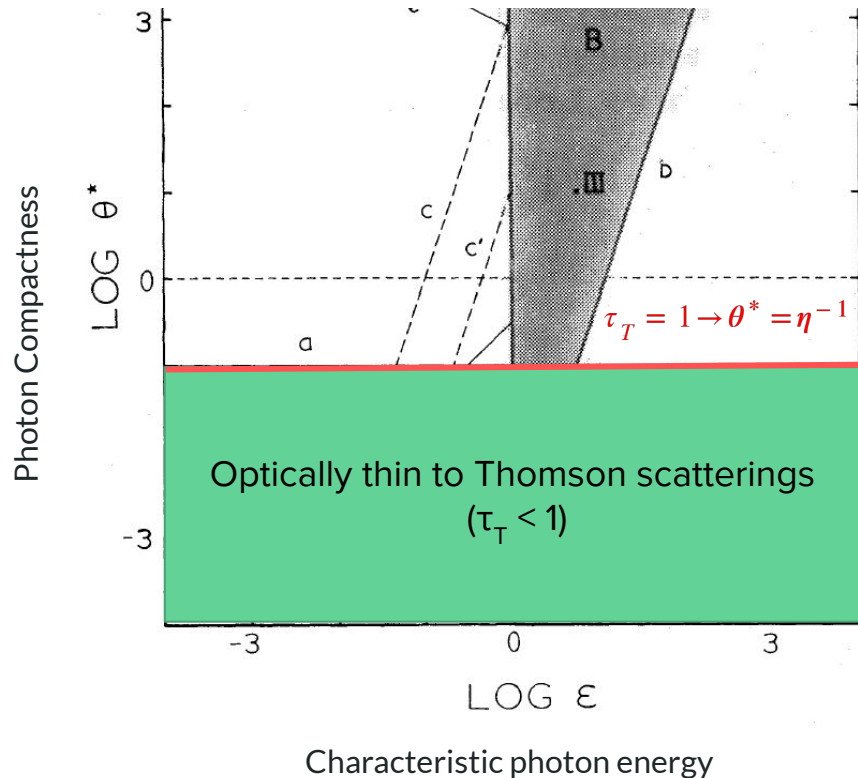
Optical depth to Thomson scatterings: $\tau_T = n_e \sigma_T R = \frac{M_i}{V m_p} \sigma_T R = \frac{1}{\eta} \frac{E_f \sigma_T}{m_p c^2 R^2} = \frac{\theta^*}{\eta}$

Optical depth to $\gamma\gamma$ interactions: $\tau_{\gamma\gamma} = n_\gamma \sigma_{\gamma\gamma} R = \frac{E_f}{V \epsilon_i m_e c^2} \frac{\sigma_T}{\epsilon_i^2} R = \frac{m_p}{m_e} \frac{\theta^*}{\epsilon_i^3} \sim 184 \frac{\theta_2^*}{(\epsilon_{i,1})^3}$

Photon compactness: $\theta^* \equiv \frac{\sigma_T L}{m_p c^3 R} = \frac{E_f \sigma_T}{m_p c^2 R^2} \sim 440 \frac{E_{f,38}}{R_7^2}$

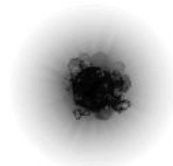
Dimensionless measure of radiation energy density !

Cosmic Fireballs

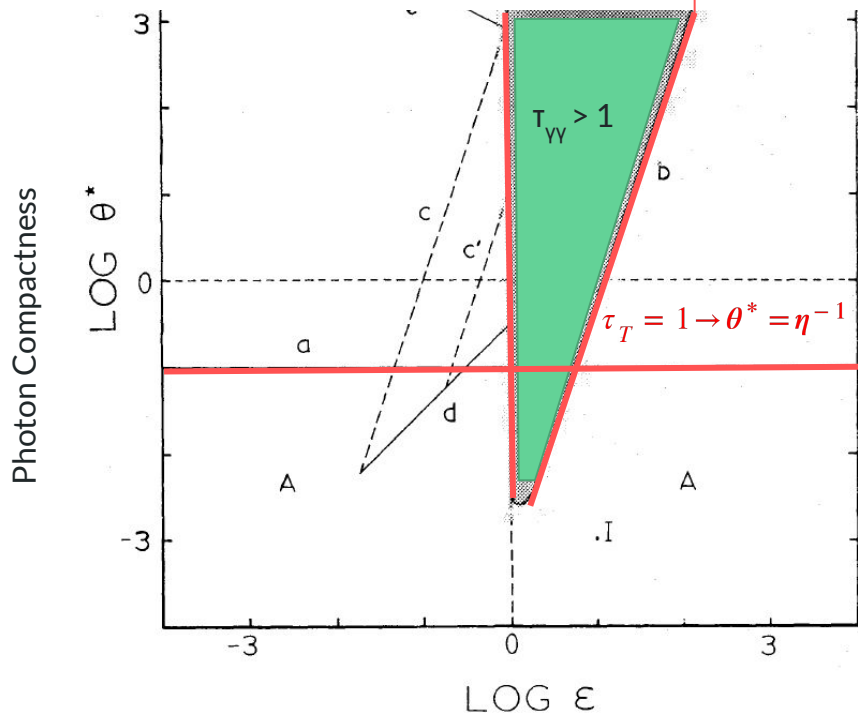


Region A

- Radiation escapes on a timescale R/c
- Photon spectrum reflects the photon production processes
- No spectral modifications due to scatterings



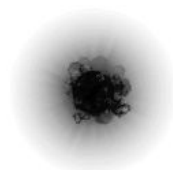
Cosmic Fireballs



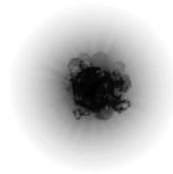
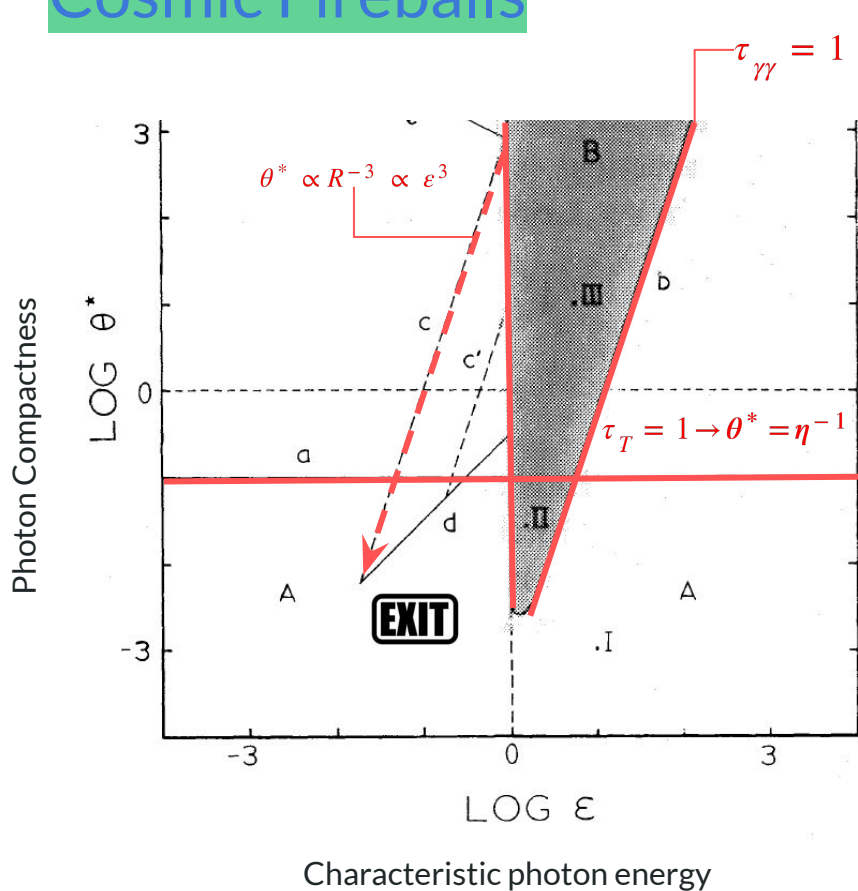
Characteristic photon energy

Region B

- $\gamma + \gamma \leftrightarrow e^- + e^+ \rightarrow$ lepton-photon gas with the same temperature
- Timescale $t_{\gamma\gamma} \ll$ timescale for photon escape and photon creation
- New photons from bremsstrahlung on $t_{\text{brem}} > t_{\gamma\gamma} \rightarrow$ more particles share the same total energy $\rightarrow$ individual photon energy drops !



Cosmic Fireballs



Region B

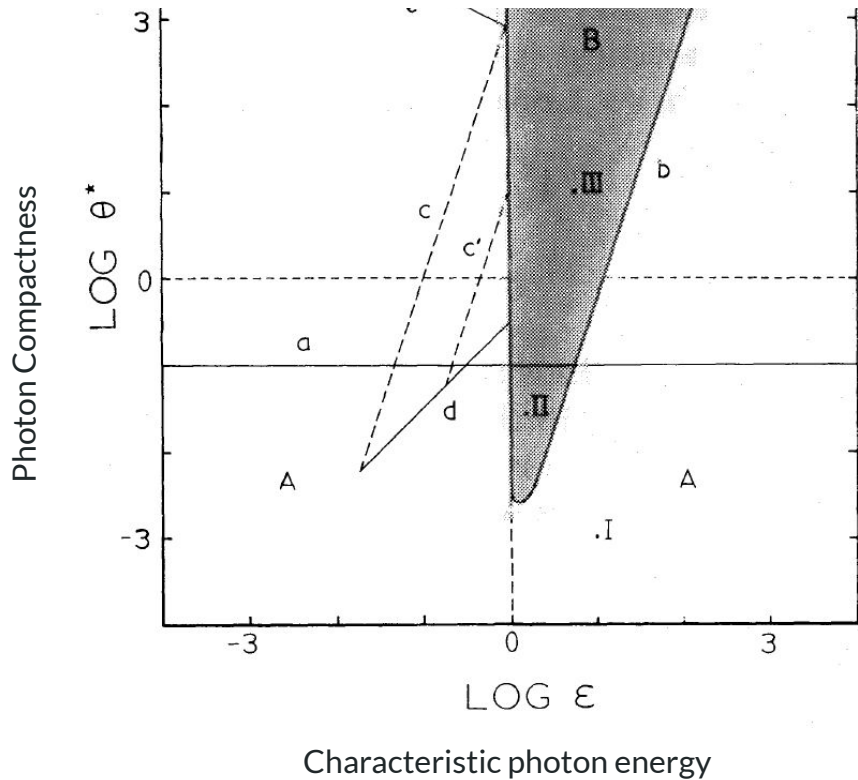
- Photons escape: $t_{\gamma, \text{diff}} \sim t_{\text{exp}} \rightarrow R_{\text{esc}} \sim R_i (\tau_{T,i})^{\frac{1}{2}} \eta^{\frac{1}{4}}$

- Escaping photon luminosity:

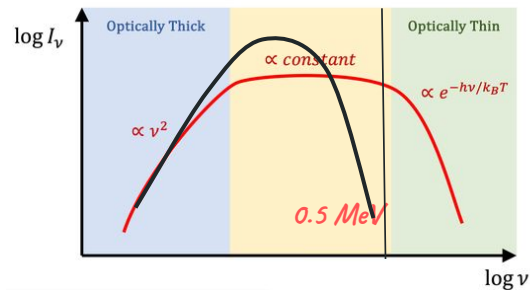
$$L_{\text{esc}} \sim \frac{E_{f, \text{esc}}}{t_{\gamma, \text{diff}}} \sim E_{f,i} \left(\frac{R_i}{R_{\text{esc}}} \right) \frac{c}{R_{\text{esc}} \tau_{T, \text{esc}}} \sim \eta \frac{R_i}{\sigma_T} m_p c^3$$

$$\theta_{\text{esc}}^* \sim \eta \left(\frac{R_i}{R_{\text{esc}}} \right) = \eta^{\frac{3}{4}} (\tau_{T,i})^{-\frac{1}{2}} \ll 1$$

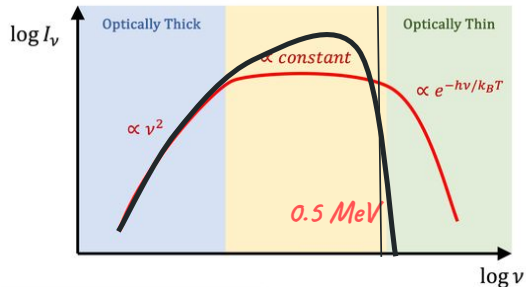
Cosmic Fireballs



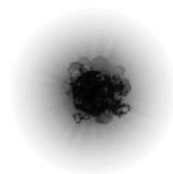
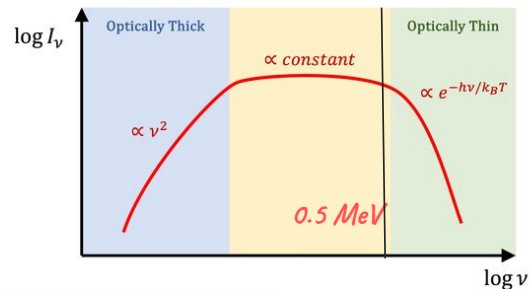
Region III



Region II



Region I



Disclaimer! These are not realistic spectra.

The “Great Debate” of 1995

... which lasted about two decades (1973 - 1997*)

Schedule

1:00 pm

Introductory Lectures

Opening: Robert Nemiroff (2 minutes)

Lecture: The 1920 Shapley - Curtis Discussion: Background, Issues, and Outcome; Virginia Trimble (40 minutes)

Lecture: Gamma-Ray Bursts: A Brief Introduction; Gerald Fishman (40 minutes)

Intermission

2:30 pm

Debate

Moderator: Sir Martin Rees

Opening Argument: Bohdan Paczynski (Cosmological viewpoint, 20 minutes)

Opening Argument: Donald Lamb (Galactic viewpoint, 20 minutes)

Rebuttal: Bohdan Paczynski (15 minutes)

Rebuttal: Donald Lamb (15 minutes)

Martin Rees Question to Donald Lamb (5 minutes)

Martin Rees Question to Bohdan Paczynski (5 minutes)

Closing Statement: Donald Lamb (10 minutes)

Closing Statement: Bohdan Paczynski (10 minutes)

Questions and Comments from the Open Floor (time remaining)

4:10 pm

Closing: Martin Rees

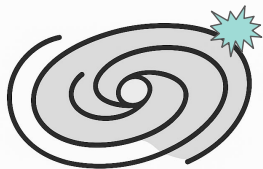
Announcements: Robert Nemiroff



Paczynski, Rees, and Lamb



The “Great Debate” of 1995

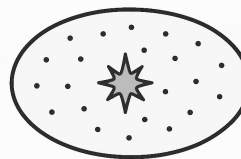


Lamb's school
(University of Chicago)

- Galactic sources
- Moderate required energetics:
 $\approx 10^{37} - 10^{40}$ erg
- Starquakes/magnetospheric flares from pulsars/magnetars
- Anisotropic distribution (e.g. disk)



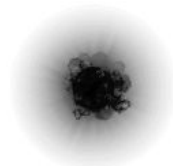
Paczynski, Rees, and Lamb



Paczynski's school
(Princeton University)

- Extragalactic sources
- Extreme required energetics:
 $\approx 10^{51} - 10^{54}$ erg $\gg$ Solar EM power released in 10 Gyrs !!
- Collapse of AGN cores ??
- Isotropic distribution

The “compactness” problem



If GRBs were found at cosmological distances $\rightarrow$ opacity to $\gamma\gamma$ pair production would be huge ! (see also Ruderman 1975, AAS) $\rightarrow$ Emergent photon spectra would be “soft” thermal $\rightarrow$ Inconsistent with observed non-thermal spectra

Photon compactness: $\theta^* \sim 4.4 \cdot 10^{16} \frac{E_{f,52}}{R_7^2}$

Opacity to $\gamma\gamma$: $\tau_{\gamma\gamma} \sim 1.8 \cdot 10^{16} \frac{\theta_{16}^*}{(\epsilon_{i,1})^3}$

Relativistic fireballs!

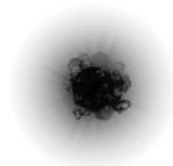
(e.g. Goodman 1986, ApJ;
Paczynski 1986, ApJ)

$$\begin{aligned} R &\sim 2 \Gamma^2 \Delta t_{obs} \\ \epsilon' &= \frac{\epsilon}{\Gamma} \end{aligned}$$

$$\tau_{\gamma\gamma} \propto \Gamma^{-2\alpha-4} \frac{E_f}{\Delta t_{obs}^2} \rightarrow \tau_{\gamma\gamma} < 1 \Rightarrow \Gamma > 100$$

Relativistic Fireballs

- Key assumptions:
- Relativistic lepton-photon plasma ($kT \gg m_e c^2$)
- Spherical symmetry
- Stationary flows



Equation of State equation

$$e = \frac{1}{\hat{\gamma} - 1} \frac{P}{\rho_0} \xrightarrow{\hat{\gamma} = \frac{4}{3}} e = 3 \frac{P}{\rho_0} \quad (1)$$

Mass continuity equation

$$\frac{\partial}{\partial t}(\gamma \rho_0) + \vec{\nabla} \cdot (\gamma \rho_0 \vec{u}) = 0 \Rightarrow r^2 \gamma \rho_0 c = \text{const} \quad (2)$$

Momentum equation

$$\gamma \rho_0 \left(\frac{\partial}{\partial t} + \vec{u} \cdot \vec{\nabla} \right) (\xi \gamma \vec{u}) = - \frac{dP}{dr} \Rightarrow \gamma \rho_0 c^2 \frac{d}{dr} (\xi \gamma) = - \frac{dP}{dr} \quad (3)$$

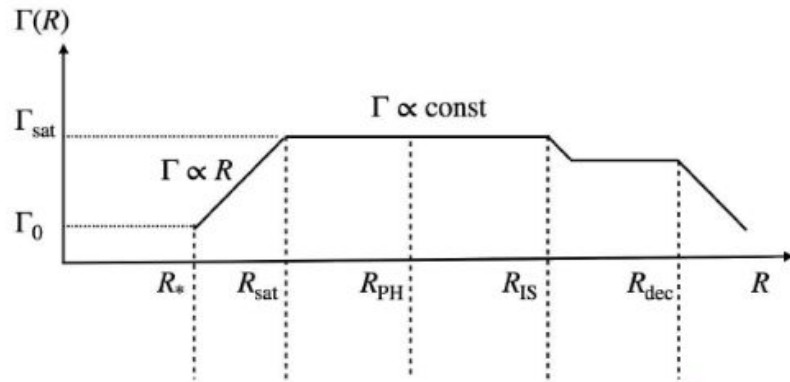
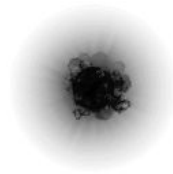
1st Law of Thermodynamics

$$\left(\frac{\partial}{\partial t} + \vec{u} \cdot \vec{\nabla} \right) \left(\frac{P}{\rho_0^{\hat{\gamma}}} \right) = 0 \Rightarrow P = K (\rho_0)^{\frac{4}{3}} \quad (4)$$

Enthalpy density (normalized)

$$\xi = 1 + \left(\frac{e}{c^2} + \frac{P}{\rho_0 c^2} \right) \xrightarrow[P \gg \rho_0 c^2]{\text{Eq. (1)}} \xi = 4 \frac{P}{\rho_0 c^2}$$

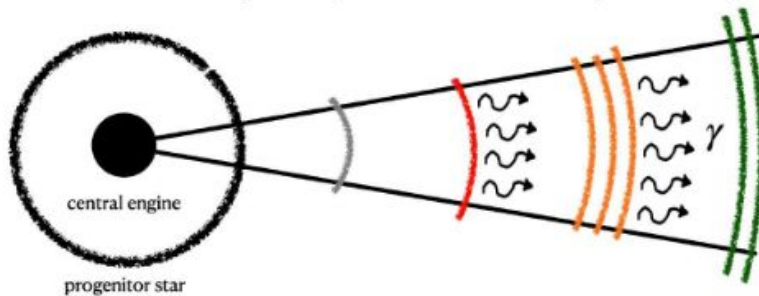
Relativistic Fireballs



Radial dependences:

$$\gamma \sim r, \quad \xi \sim \frac{1}{r}, \quad \rho_0 \sim \frac{1}{r^3}, \quad P \sim \frac{1}{r^4}, \quad T \sim \frac{1}{r}$$

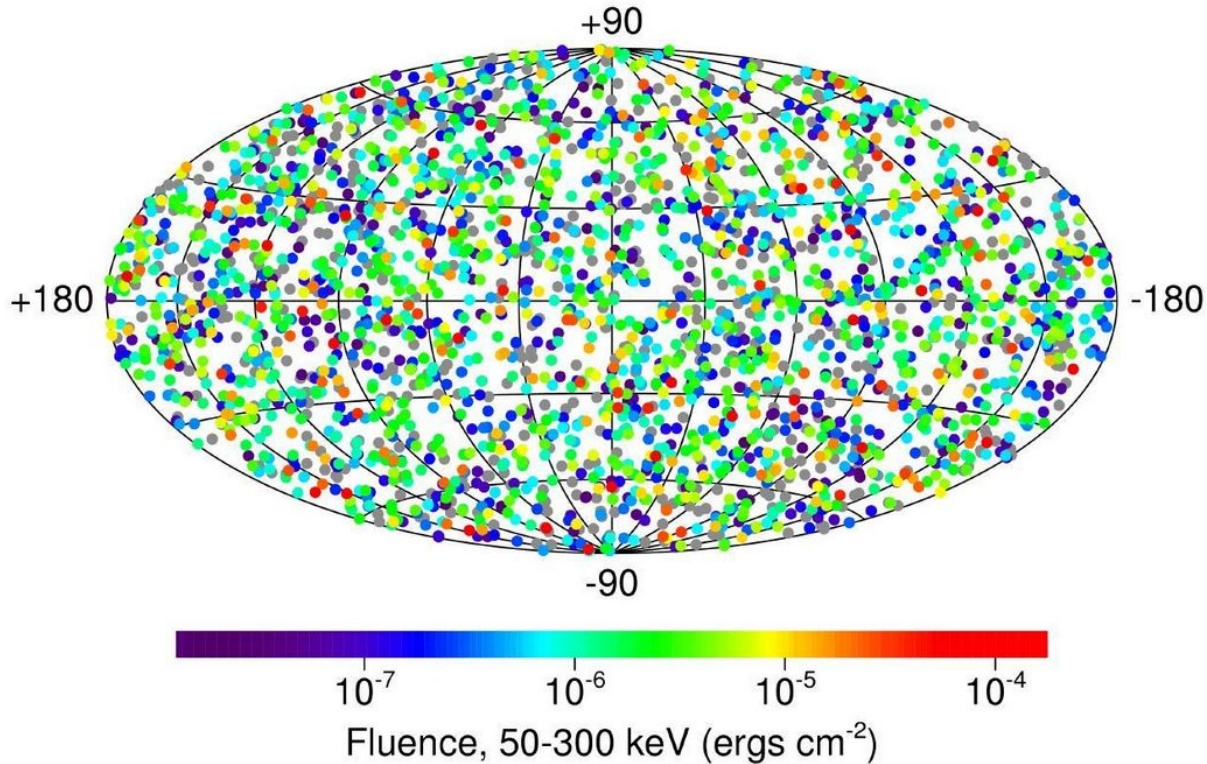
Asymptotic Lorentz factor:



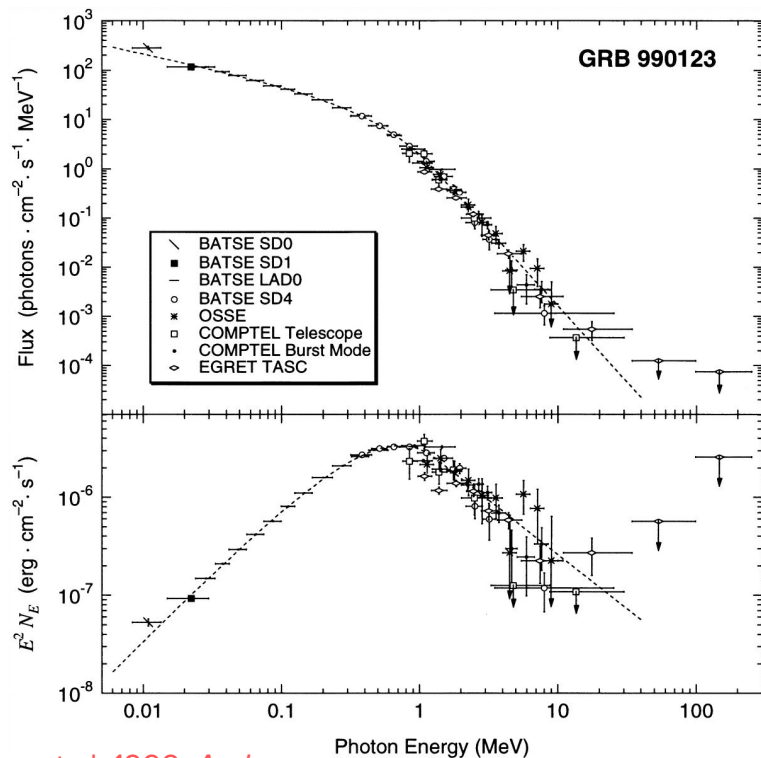
$$\gamma_i \xi_i = \gamma_\infty \xi_\infty \xrightarrow[\xi_\infty \sim 1]{\gamma_i \sim 1} \gamma_\infty = \xi_i = 4 \frac{P_i}{\rho_i c^2} = \frac{4}{3} (1 + \eta) \sim \eta \gg 1$$

The BATSE era (1991 - 2000)

2704 bursts



The BATSE era (1991 - 2000): GRB spectra



$$F_{\text{Band}}(E) = \begin{cases} A \left(\frac{E}{100 \text{ keV}} \right)^{\alpha} \exp \left(-\frac{E(2+\alpha)}{E_{\text{peak}}} \right) & E < E_c \\ A \left[\frac{(\alpha-\beta)E_{\text{peak}}}{100 \text{ keV}(2+\alpha)} \right]^{\alpha-\beta} \exp(\beta-\alpha) \left(\frac{E}{100 \text{ keV}} \right)^{\beta} & E \geq E_c \end{cases}$$

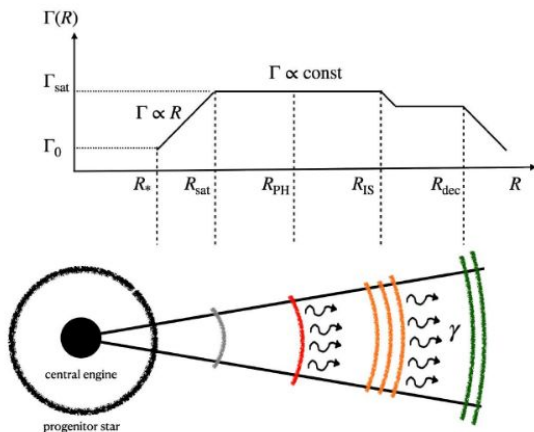
$$E_c = (\alpha - \beta) \frac{E_{\text{peak}}}{2 + \alpha} \equiv (\alpha - \beta) E_0$$

[Band et al. 1993, ApJ](#)

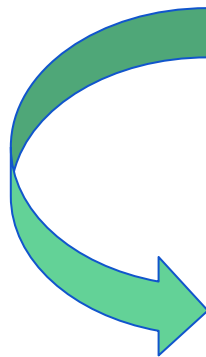
Non-thermal photon spectra → optically thin
plasmas → relativistic motions

Synchrotron GRB models

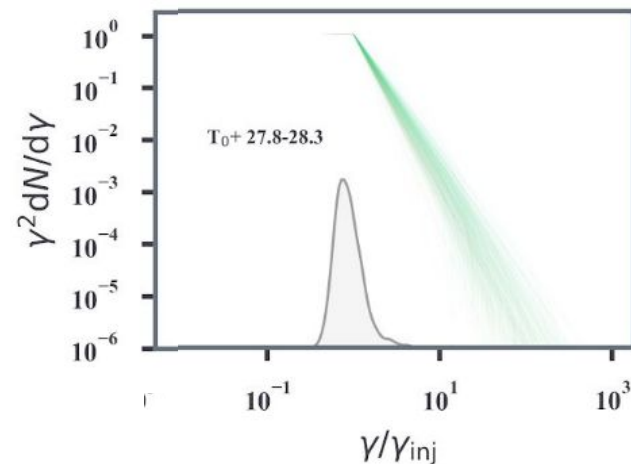
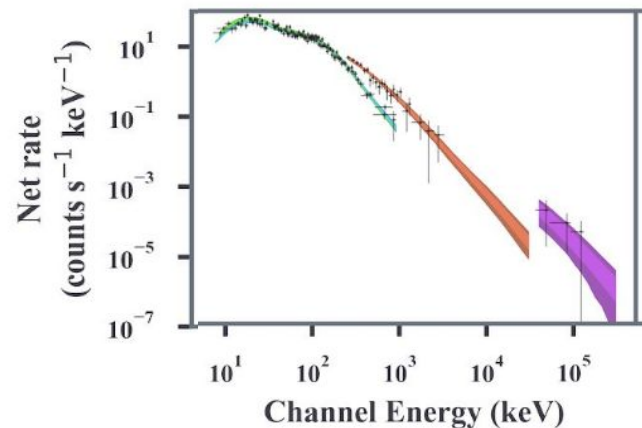
- Synchrotron radiation from relativistic electrons
- Emission from $R > R_{\text{ph}}$
- Jet coasting with $\Gamma = \text{const.}$



Detector
photon
spectra



Electron
distribution
in GRB jet



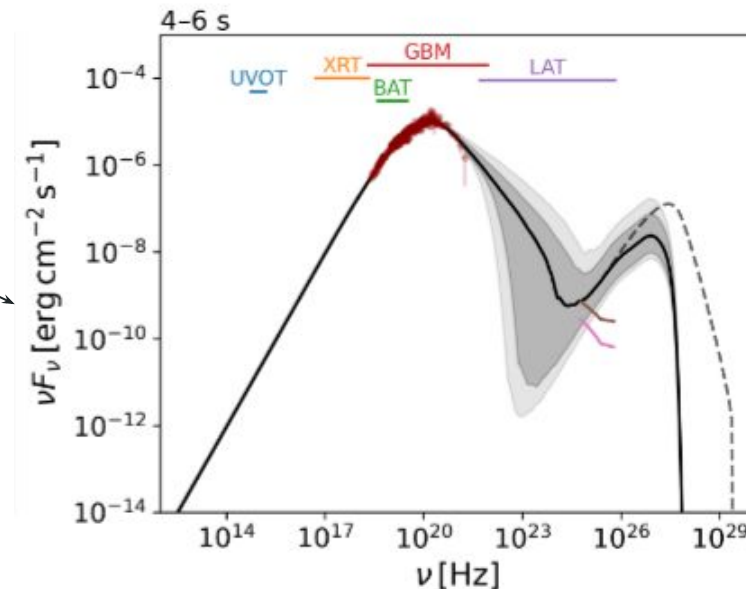
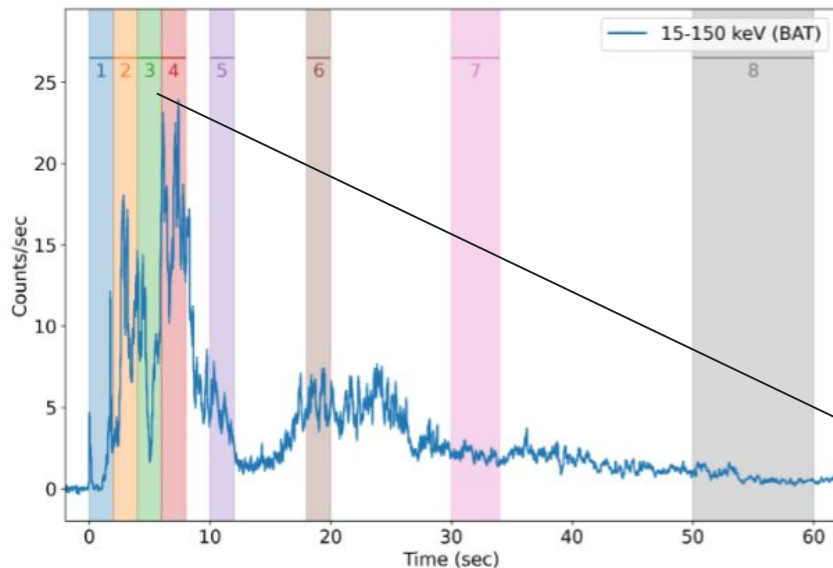
An example: GRB 211211A

Stathopoulos et al. 2024, A&A

<https://github.com/mariapetro/LeHaMoC/>

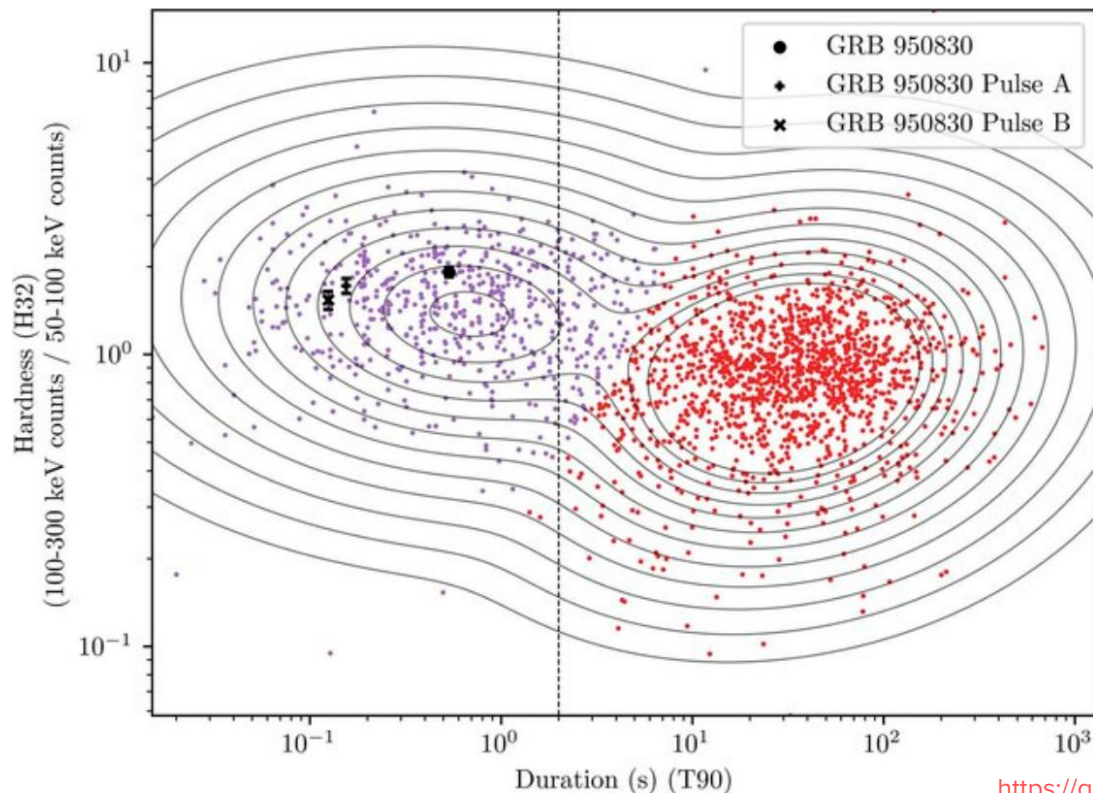


- Numerical SSC models
- MCMC fits



Petropoulou, Gkoni, Xyloportas et al. , in prep.

The BATSE era (1991 - 2000): GRB durations



- Bimodal distribution in durations
- Short GRBs (< 2 sec) have harder photon spectra
- Long GRBs (> 2 sec) have softer photon spectra
- Bimodality $\rightarrow$ different progenitors

See also [Kouveliotou et al. 1993, *ApJ*](https://ui.adsabs.org/abs/1993ApJ...401..680K)



GRB progenitors

Stellar collapsars



[McFadyen & Woosley 1999, ApJ](#); [Woosley & Bloom 2006, ARA&A](#)

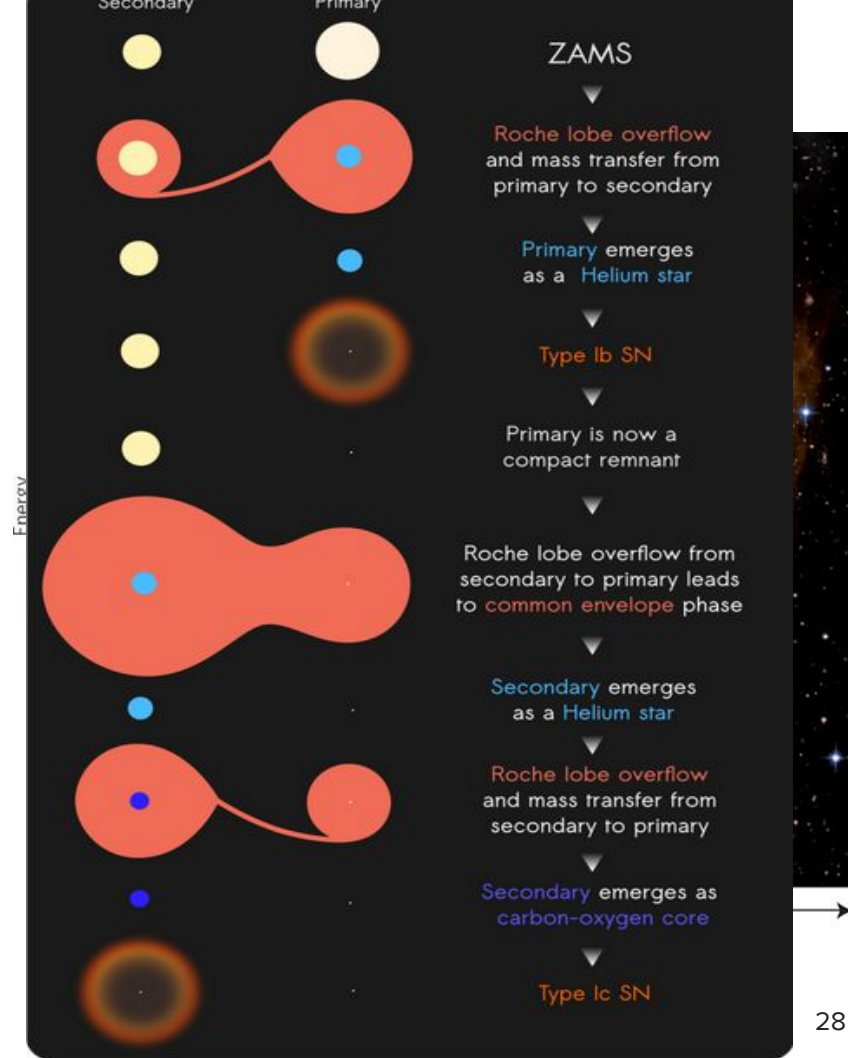
NS-NS or NS-BH mergers



[Eichler et al. 1989, Nature](#) ; [Narayan et al. 1992, ApJL](#)

Collapsars

- **Key discovery:** SN 1998bw with GRB 980425
([Bloom et al. 1999, Nature](#))
- GRBs associated with **SNe Type Ib/c** (no H, no He lines) → stripped stars
- GBR-selected SNe have broad lines → associated with fast ($\sim 0.1 c$) outflows
- All GBR-selected SNe are Type Ib/c-BL

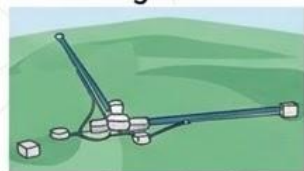


Mergers

Key discovery: GW 170817 with GRB 170817A
([Abbott et al. 2017, ApJ](#), [Troja et al 2017, Nature](#))



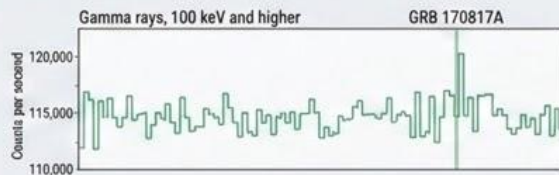
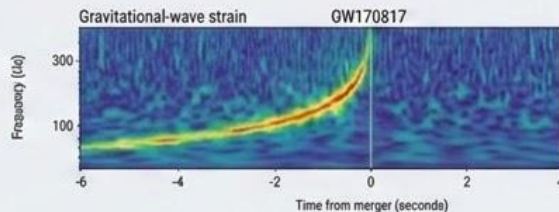
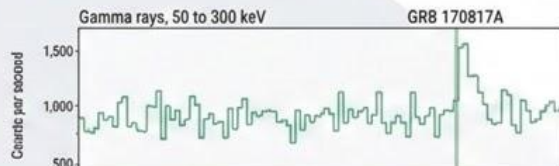
Fermi



LIGO-Virgo



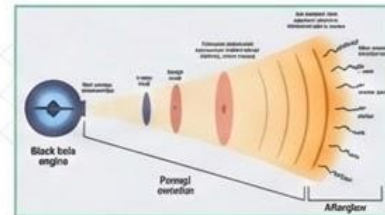
INTEGRAL



NS merger



Short GRB

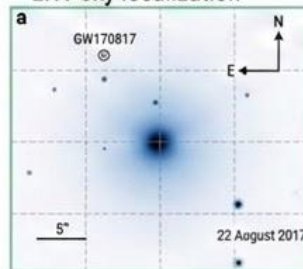


X-ray

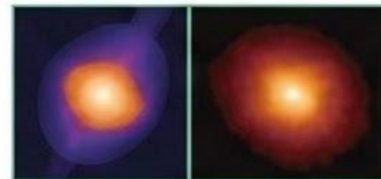
Radio afterglow



LHV sky localization



UV/Optical/NIR Kilonova



Part 2

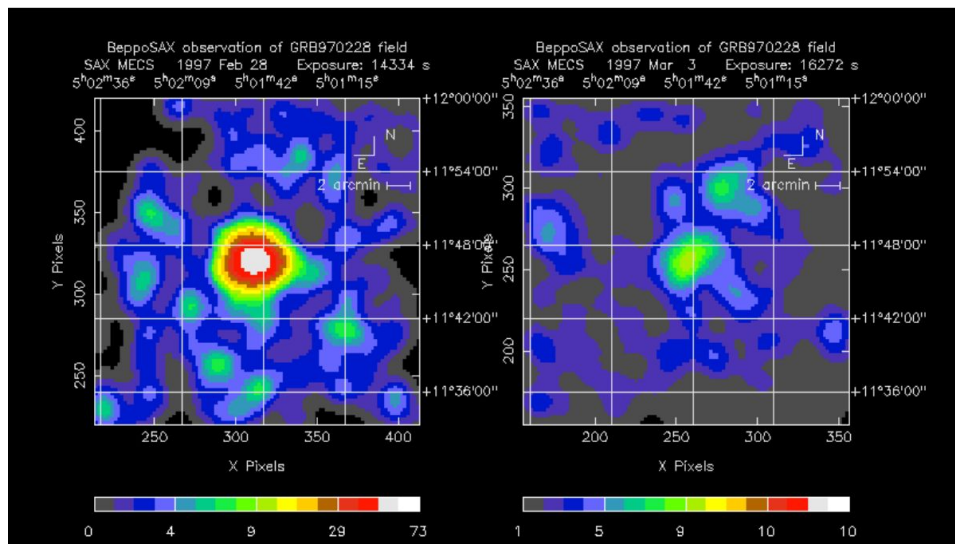


Introduction to GRBs afterglows

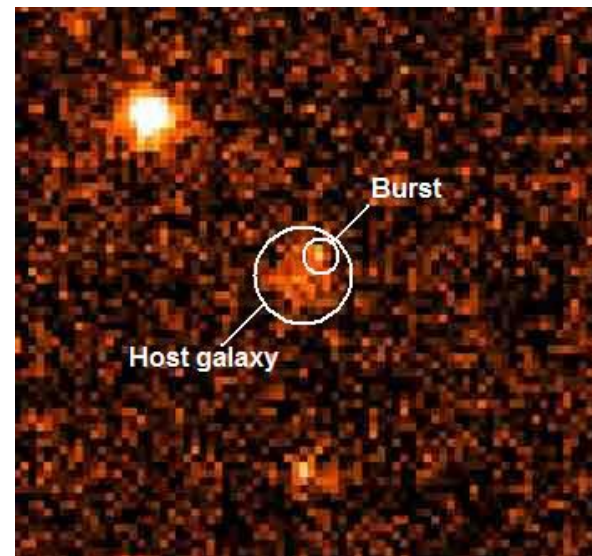
The discovery of the GRB afterglow (1997)

GRB 970228

BeppoSax (X-rays)

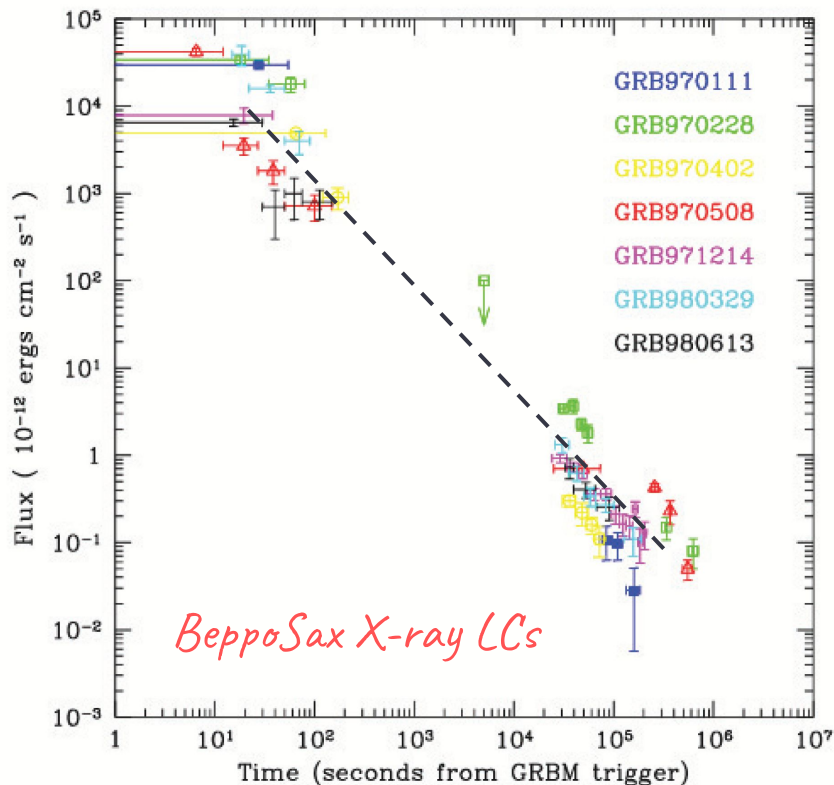


HST (optical)



- First determination of the GRB host galaxy at $z = 0.695$! → Direct evidence for extragalactic origin
- First observation of a GRB counterpart in X-ray and optical wavelengths after the γ -ray emission !

What are GRB afterglows?

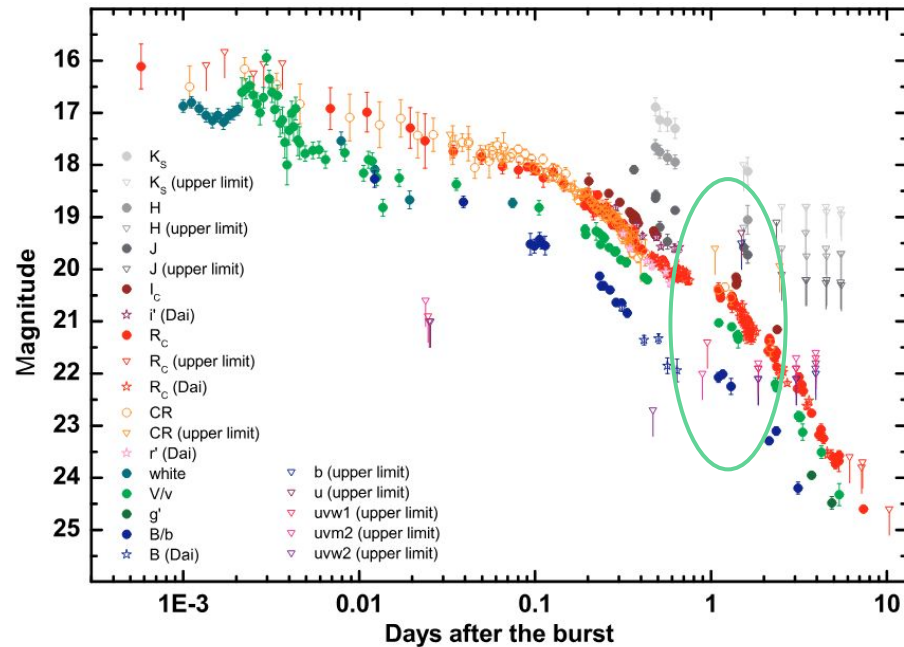
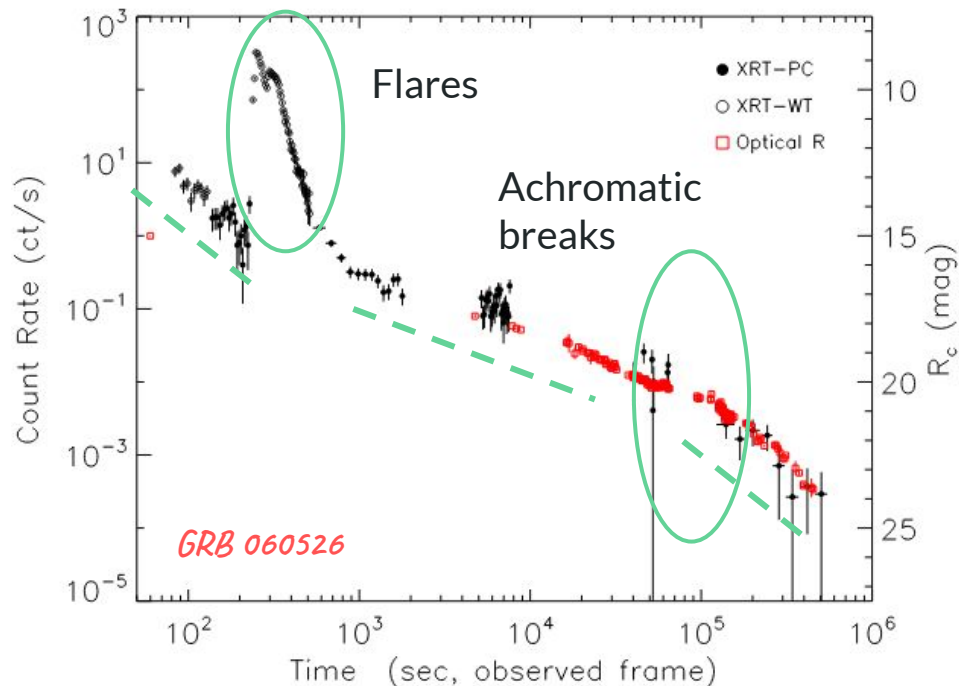


- Long-lasting (hours to months) electromagnetic emission at lower energies (X-rays, optical, radio) following the brief γ -ray flash
- Flux decays as a power law
- Key observables: peak time, peak flux, power-law index

[Costa et al. 1999, A&A Supplement Series](#)

GRB afterglows in the Swift era (2004 - today)

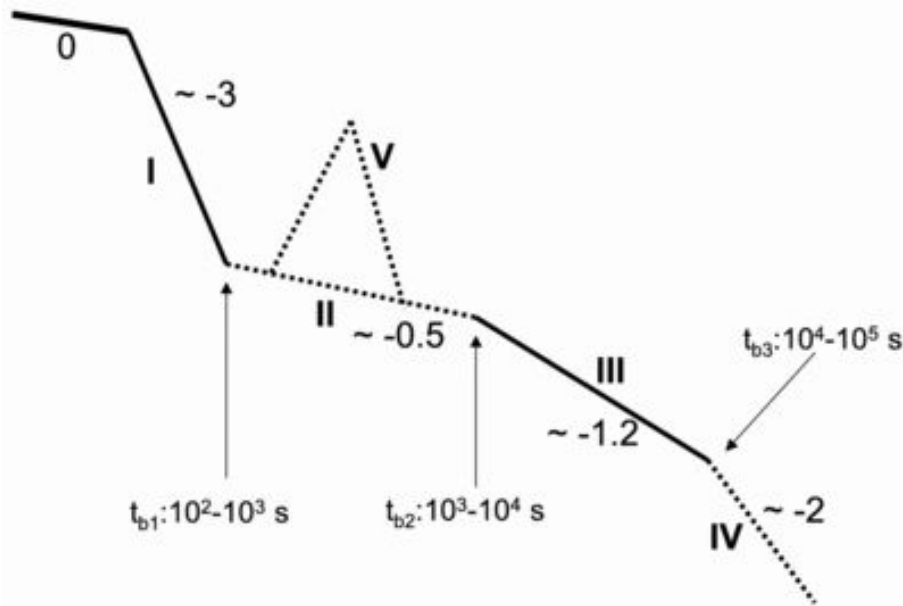
A more complex picture emerges!



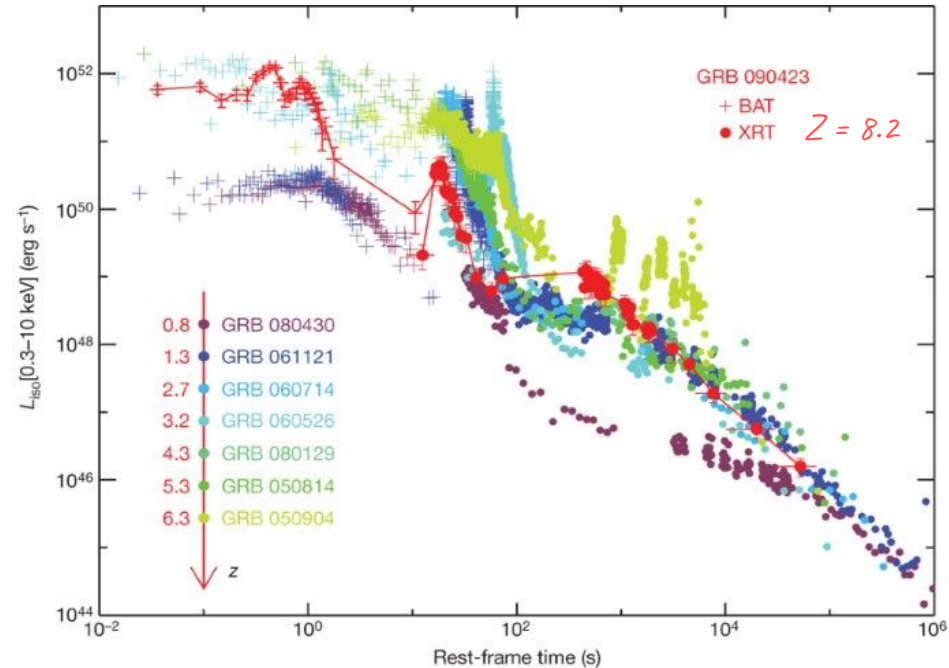
[Thöne et al. 2010, A&A](#)

GRB afterglows in the Swift era (2004 - today)

The “canonical” X-ray afterglow



[Zhang et al. 2006, ApJ](#)



[Salvaterra et al. 2009, Nature](#)

Part 3

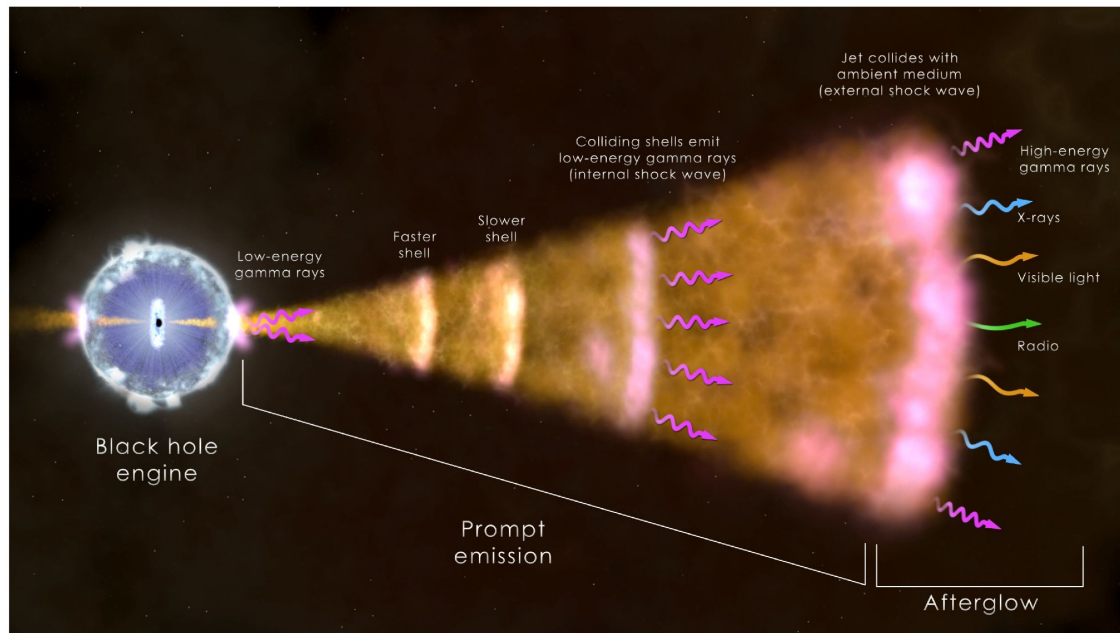


Theory of GRBs afterglows

The GRB afterglow paradigm

Key ingredients:

- Relativistic blast wave dynamics
- Relativistic beaming of radiation
- Non-thermal radiative processes
- Particle acceleration at relativistic shocks



Relativistic blast waves

Energy conservation:

$$M\Gamma c^2 + dm c^2 = (M + dM) (\Gamma + d\Gamma) c^2 \quad (1)$$

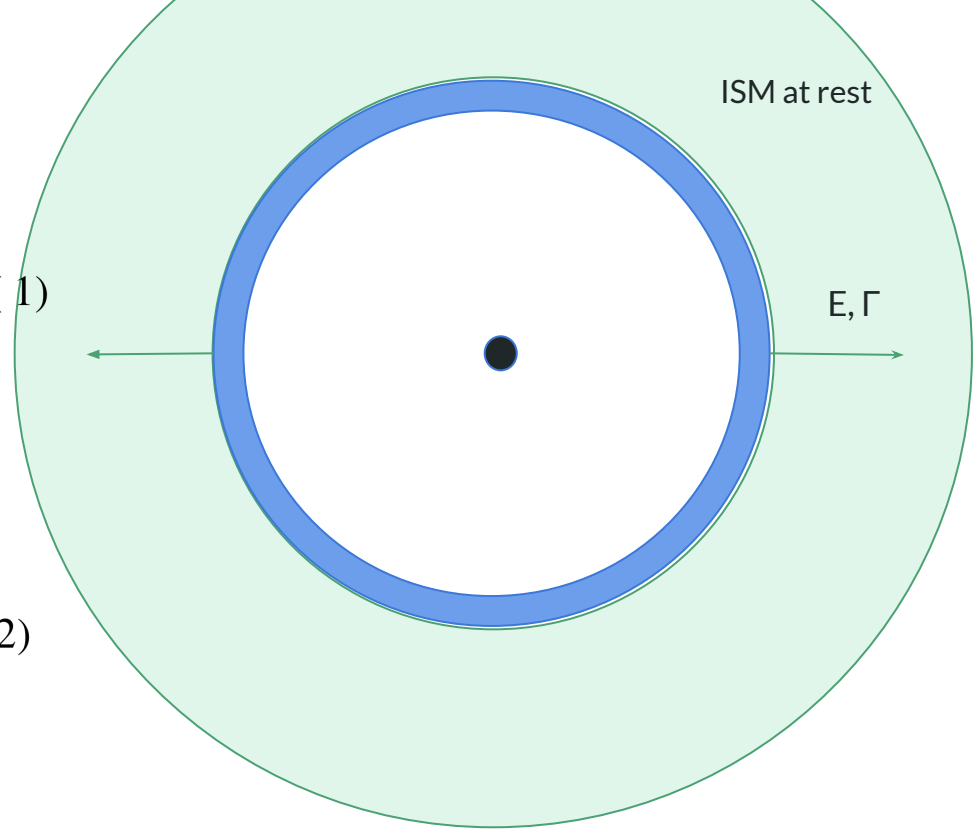
$$dm = 4\pi r^2 \rho(r) dr$$

Momentum conservation:

$$M\Gamma\beta c = (M + dM) (\Gamma + d\Gamma) (\beta + d\beta) c \quad (2)$$

$$(1), (2) \rightarrow \boxed{\frac{d\Gamma}{dm} = - \frac{\Gamma^2 - 1}{M}}$$

$$M(r) = M_0 + 4\pi \int_{r_0}^r dr' r'^2 \Gamma(r') \rho(r') \Rightarrow \boxed{dM = \Gamma(r) dm}$$



Blandford & McKee 1976, Phys. Fluids;
Chiang & Dermer 1999, ApJ

Non-radiative relativistic blast waves

Blast wave (shocked fluid) inertial mass:

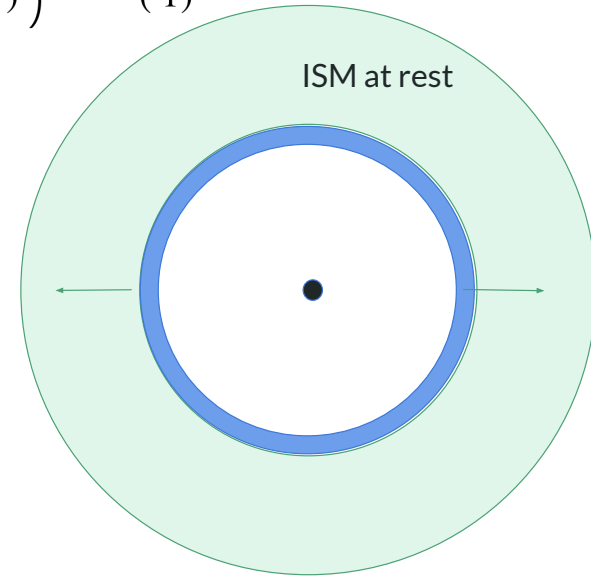
$$M(r) = \left(M_0^2 + 2\Gamma_0 M_0 M_{sw}(r) + M_{sw}^2(r) \right)^{\frac{1}{2}} \quad (1)$$

Blast wave (shocked fluid) Lorentz factor:

$$\Gamma(r) = \frac{M_{sw}(r) + \Gamma_0 M_0}{M(r)} \quad (2)$$

Swept-up mass:

$$M_{sw}(r) = 4\pi \int_{r_0}^r dr r^2 \rho(r) \quad (3)$$



Non-radiative relativistic blast waves

$$M(r) = \left(M_0^2 + 2\Gamma_0 M_0 M_{sw}(r) + M_{sw}^2(r) \right)^{\frac{1}{2}} \quad (1)$$

$$\Gamma(r) = \frac{M_{sw}(r) + \Gamma_0 M_0}{M(r)} \quad (2)$$

Regime 1: Coasting Phase

$$M_0 \gg \Gamma_0 M_{sw}$$

$$M(r) \approx M_0$$

$$\Gamma(r) \approx \Gamma_0$$

Regime 2: Deceleration Phase

$$\frac{M_{sw}}{\Gamma_0} < M_0 < 2\Gamma_0 M_{sw}$$

$$M(r) \approx \sqrt{2\Gamma_0 M_0 M_{sw}(r)} \propto r^{\frac{3}{2}}$$

$$\Gamma(r) \approx \Gamma_0 \left(\sqrt{\frac{M_0}{2\Gamma_0 M_{sw}(r)}} + \dots \right) \propto r^{-\frac{3}{2}}$$

Regime 3: Newtonian Phase

$$M_{sw} > 2\Gamma_0 M_0$$

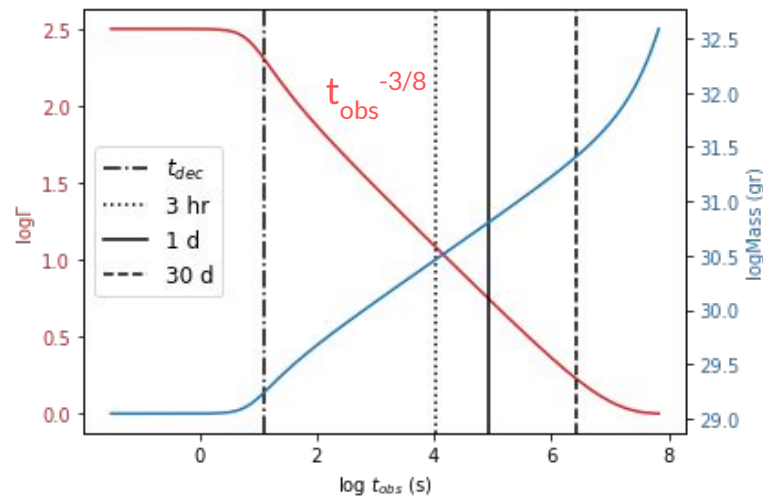
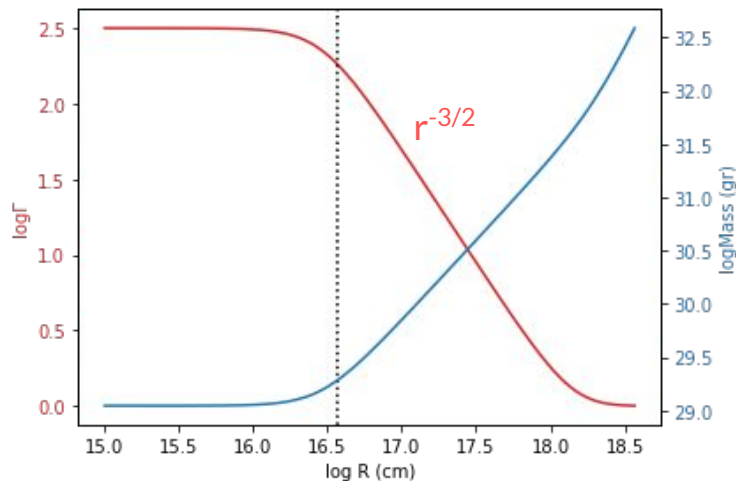
$$M(r) \approx M_{sw}(r) \propto r^{\frac{3}{2}}$$

$$\Gamma(r) \approx 1 + \Gamma_0 \frac{M_0}{M_{sw}(r)}$$

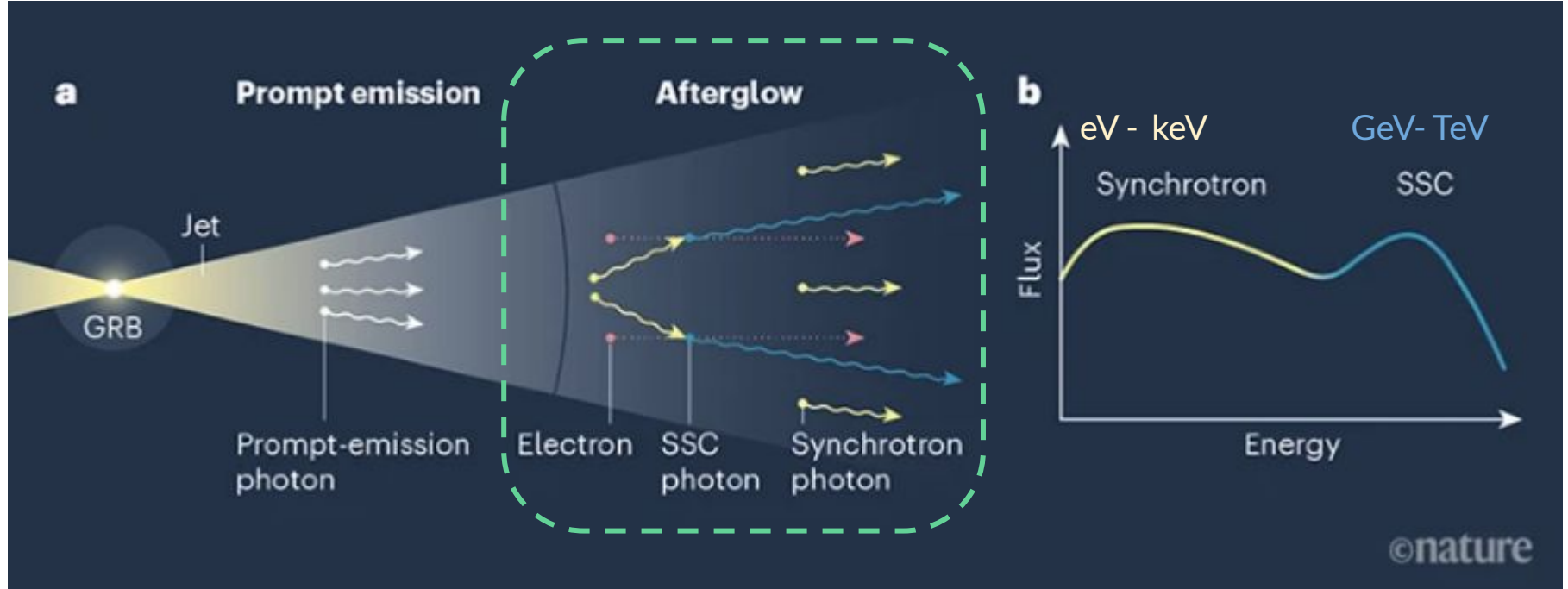
Non-radiative relativistic blast waves

Deceleration radius: $\Gamma_0 M_{sw}(r_{dec}) \sim M_0 \Rightarrow r_{dec} = \left(\frac{3E_0}{4\pi n m_p \Gamma_0^2 c^2} \right)^{\frac{1}{3}} \approx 10^{16.5} \text{ cm} \left(\frac{E_{0,52.5}}{n_0 \Gamma_{0,2.5}} \right)^{\frac{1}{3}}$

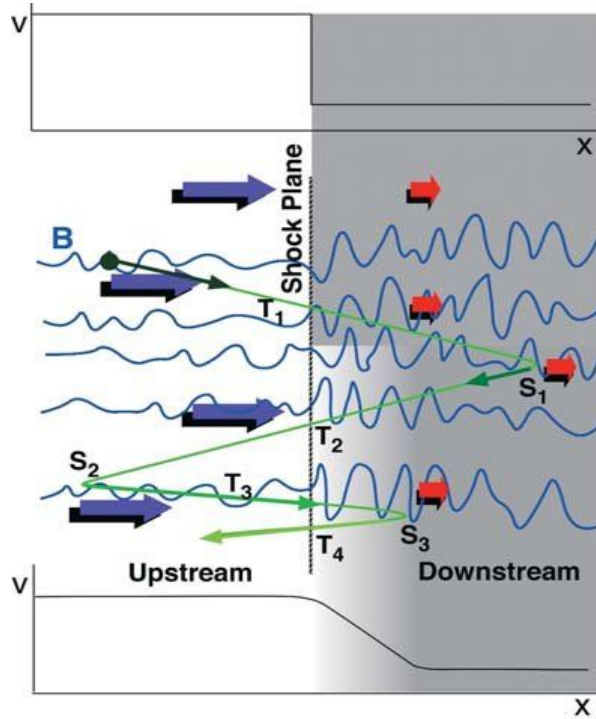
Deceleration time: $t_{dec} \sim \frac{r_{dec}}{c \Gamma_0^2} \propto E_0^{\frac{1}{3}} n_0^{-\frac{1}{3}} \Gamma_0^{-\frac{8}{3}}$



Radiative processes



Particle acceleration



- Shocks dissipate bulk kinetic energy $\rightarrow$ internal energy, non-thermal particle energy
- **Fermi** acceleration $\rightarrow$ particles gain energy via multiple scatterings across a velocity gradient (there is also shock-drift, ...)
- **Scatterings mediated by magnetic fields** $\rightarrow$ generated by instabilities
- Shocks can accelerate particles into **power-law** distributions.
- Inefficient acceleration in
 - Superluminal shocks
 - High - σ plasmas

Relativistic shock acceleration

$$\sigma = 0$$

$$\gamma_0 = 15$$

Low- σ shocks:

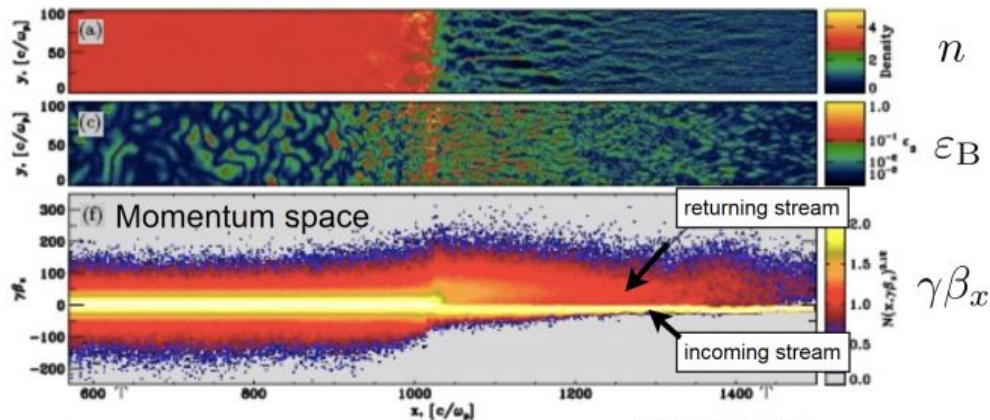
- returning particles
- filamentation instabilities

$$\sigma = 0.1$$

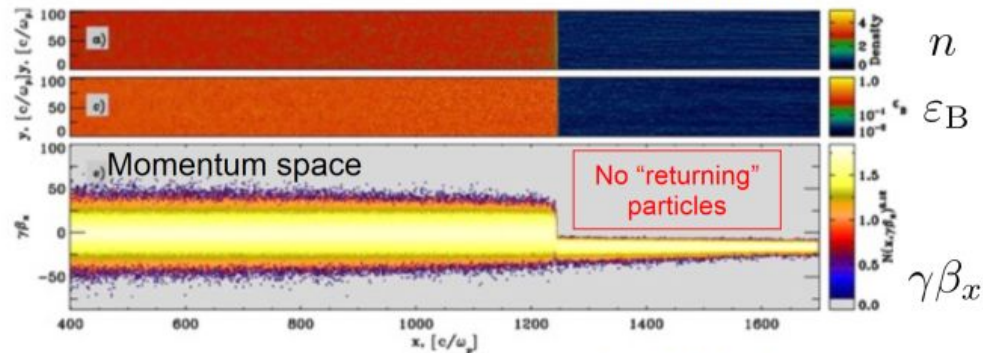
$$\gamma_0 = 15$$

High- σ shocks:

- no returning particles
- no turbulence



Sironi et al. 2013

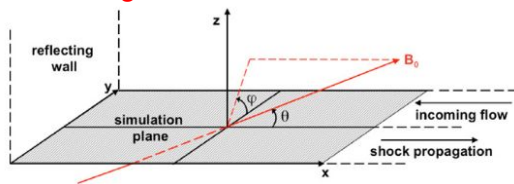


Sironi & Spitkovsky
2011

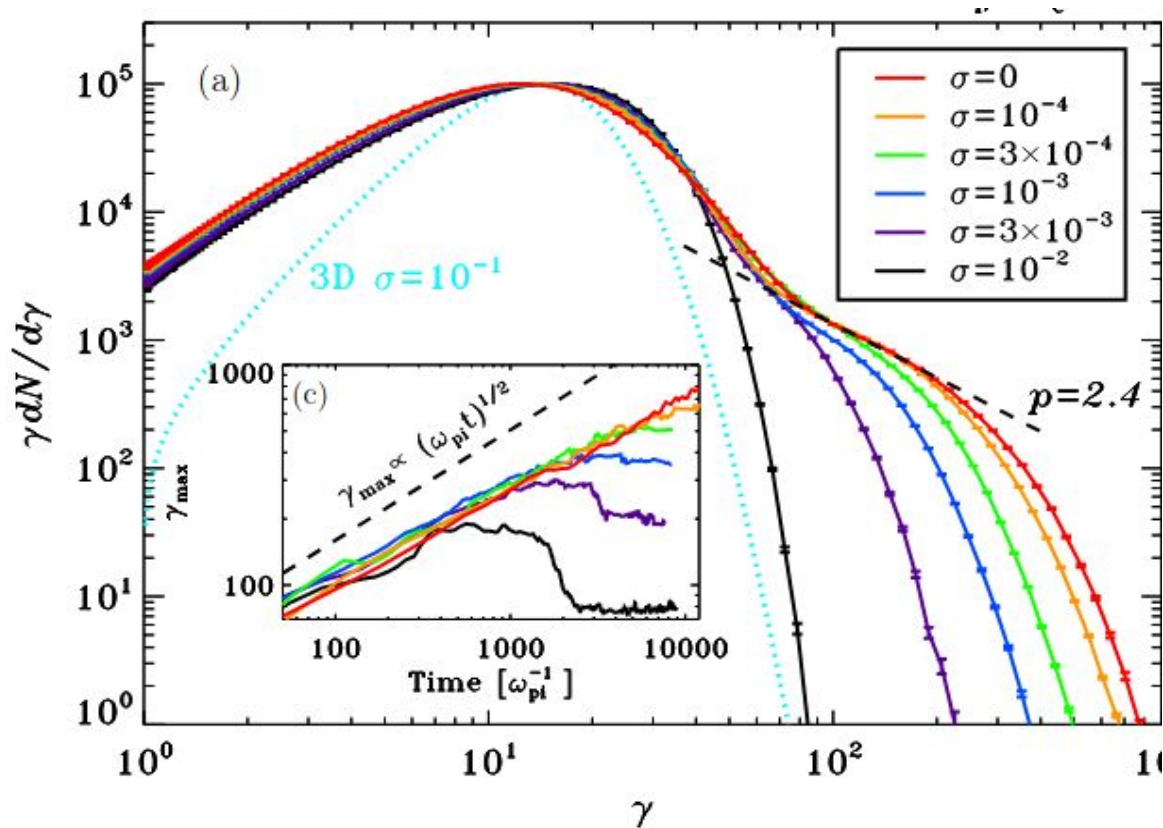
← weakly magnetized
(relevant to GRB blast waves)

← strongly magnetized
(relevant to internal shocks in jets)

$$\theta = 15 \text{ deg}$$



Relativistic shock acceleration



Diffusion coefficient and maximal energy depend on typical scale λ of turbulent magnetic field :

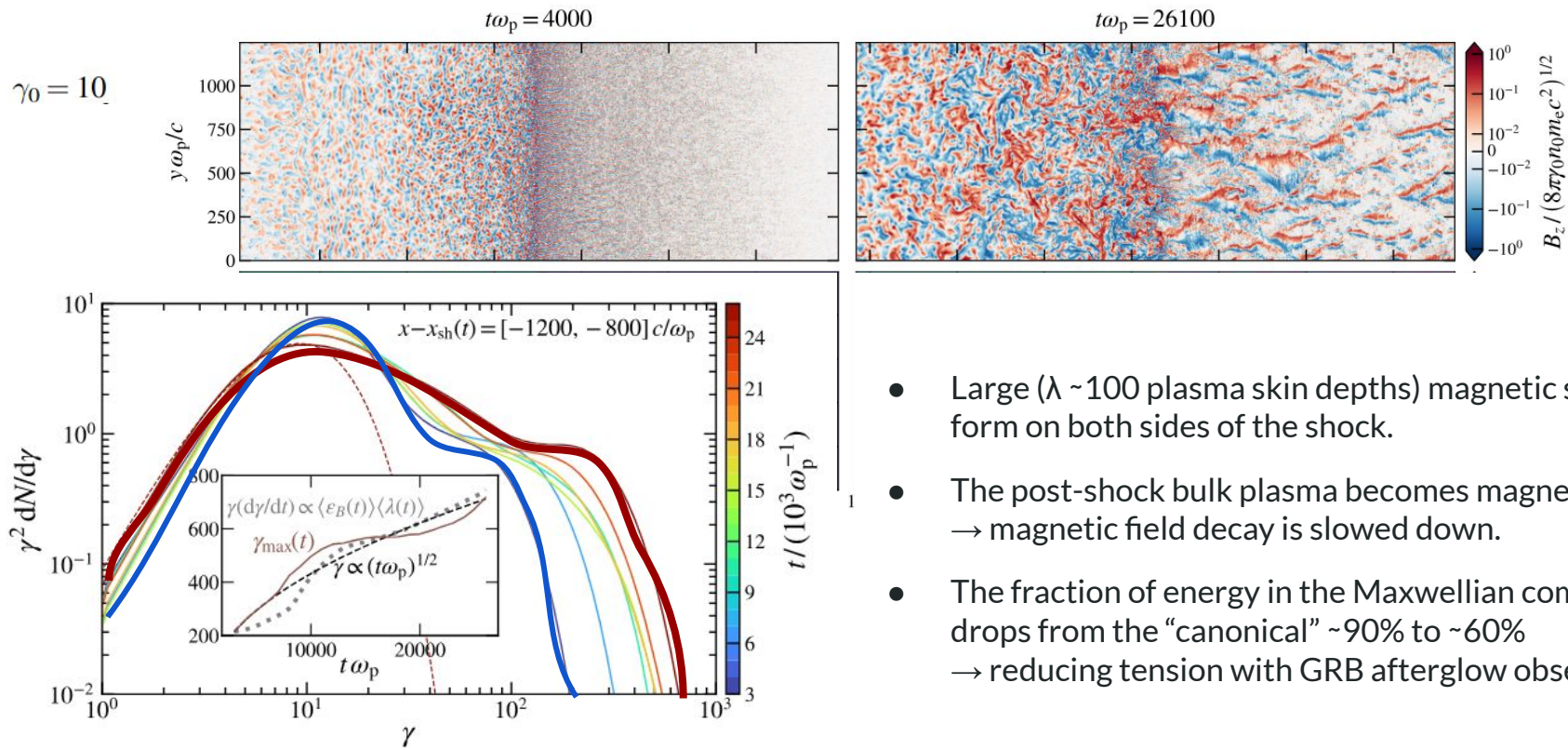
$$D(\varepsilon) \sim c\lambda \left[\frac{r_L(\varepsilon)}{\lambda} \right]^2 = c\lambda \left(\frac{\varepsilon}{eB\lambda} \right)^2$$

$$\gamma_{\max} m_i c^2 \sim eB\lambda \left(\frac{ct}{\lambda} \right)^{1/2}$$

Some problems:

1. Slow increase of $\gamma_{\max}$
2. Prominent Maxwellian component in particle distribution
3. Turbulent magnetic field decays far from shock

Long term evolution of relativistic shocks



- Large ($\lambda \sim 100$ plasma skin depths) magnetic structures form on both sides of the shock.
- The post-shock bulk plasma becomes magnetized $\rightarrow$ magnetic field decay is slowed down.
- The fraction of energy in the Maxwellian component drops from the “canonical” $\sim 90\%$ to $\sim 60\%$ $\rightarrow$ reducing tension with GRB afterglow observations.

The standard GRB afterglow model

Power entering the shocked plasma:

$$\frac{dE}{dt} = \beta c \cdot (\Gamma - 1) \Gamma \rho c^2 \cdot 4\pi r^2$$

Electron distribution:

$$\frac{dN}{dtd\gamma} = K_e \gamma^{-p}, \quad \gamma_{min} \leq \gamma \leq \gamma_{max}, \quad \gamma_{min} \sim \frac{m_p}{m_e} \Gamma(r)$$

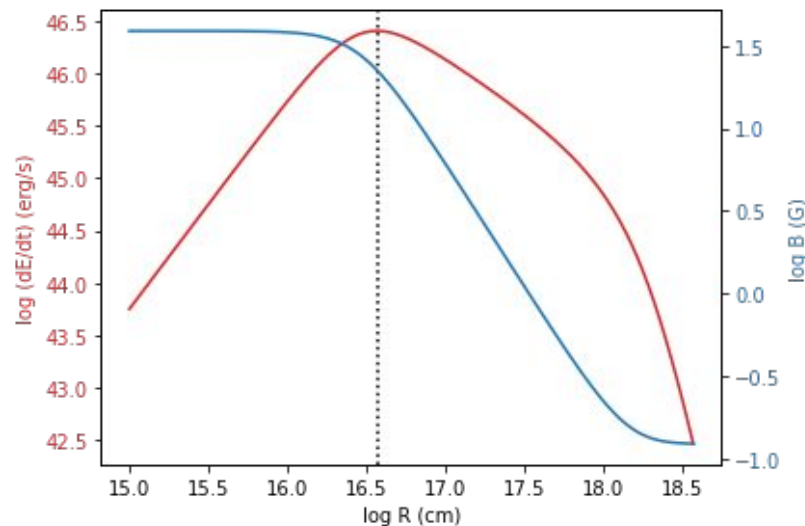
Power injected into relativistic electrons:

$$L_e = m_e c^2 \int_{\gamma_{min}}^{\gamma_{max}} d\gamma (\gamma - 1) \frac{dN}{dtd\gamma} = \epsilon_e \frac{dE}{dt}$$

Magnetic field strength:

$$\frac{B^2}{8\pi} = \epsilon_B u_{sh} = \epsilon_B 4\Gamma(r) \rho (\Gamma - 1) c^2$$

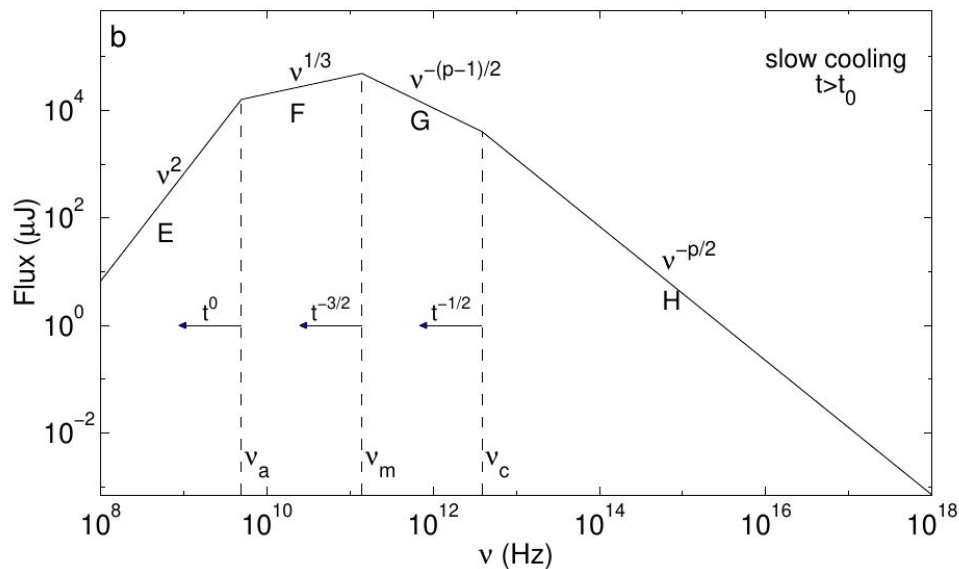
ϵ_B, ϵ_e are key free parameters!



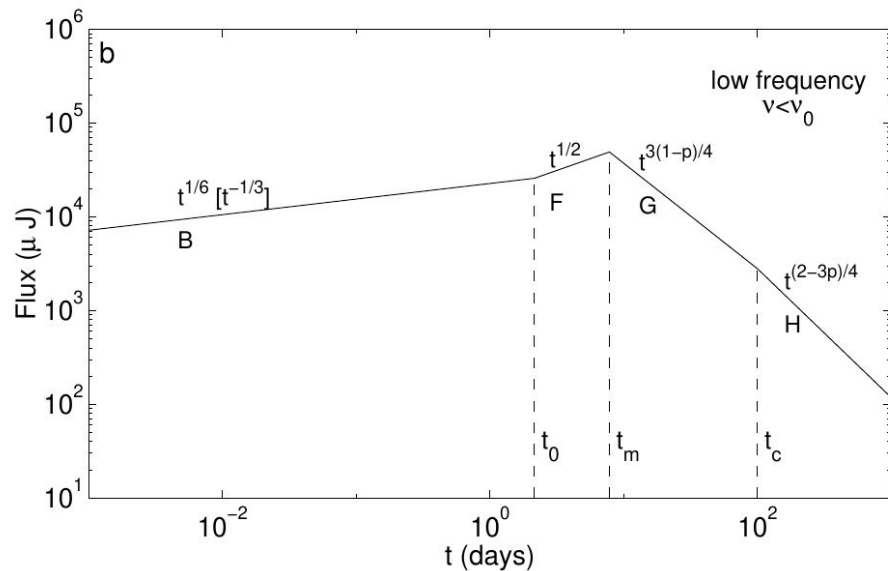
The Synchrotron GRB afterglow model

Analytical results

Synchrotron spectrum



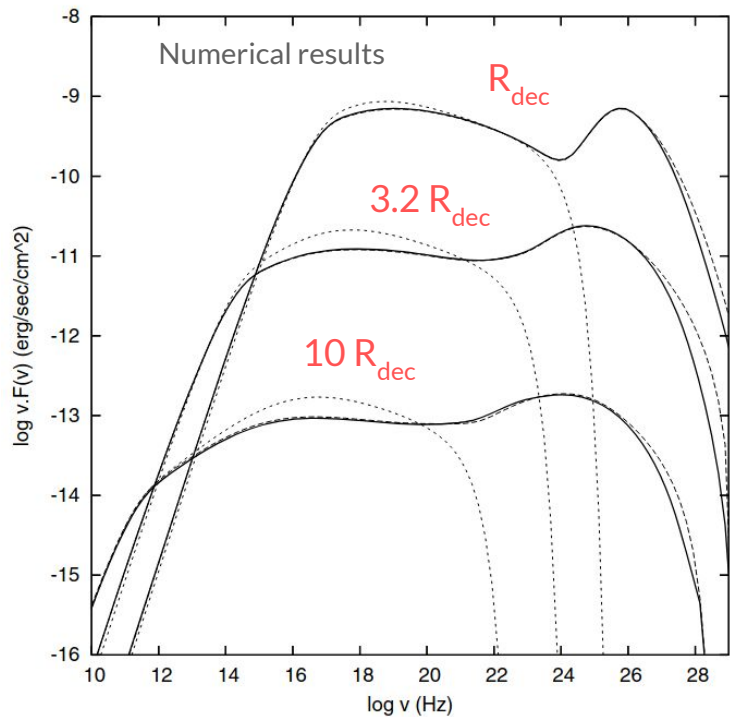
Synchrotron light curve



Sari, Piran, Narayan 1998, ApJL

The SSC afterglow models

Synchrotron self-Compton (SSC)

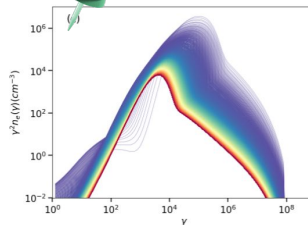


Petropoulou & Mastichiadis 2009, A&A



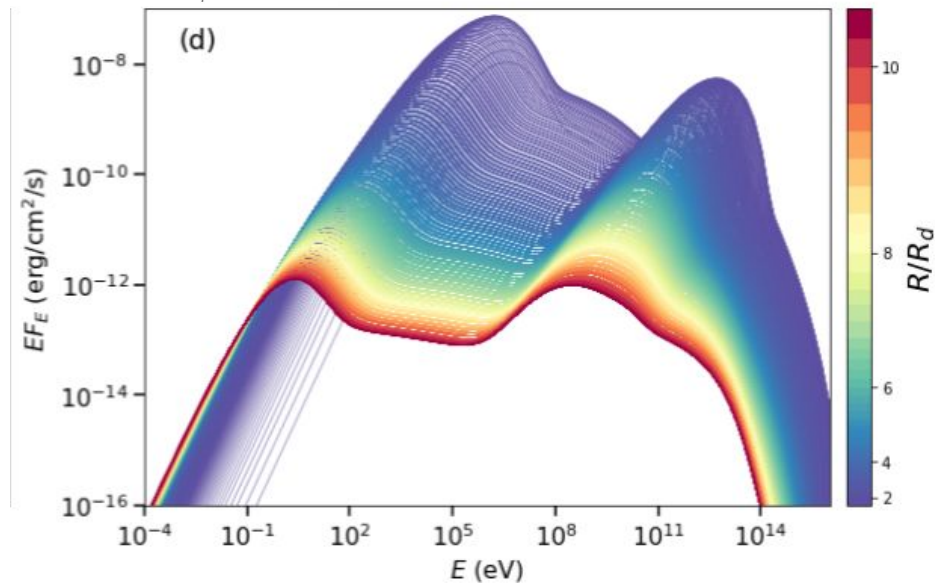
$$\frac{\partial n_e}{\partial t} + c \frac{3n_e}{r} = Q_e^{(\text{inj})} + Q_e^{(\gamma\gamma)} + \mathcal{L}_e^{(\text{ad})} + \mathcal{L}_e^{(\text{syn})} + \mathcal{L}_e^{(\text{ics})} \quad (9)$$

$$\frac{\partial n_\gamma}{\partial t} + c \frac{3n_\gamma}{r} + c \frac{n_\gamma}{r} = Q_\gamma^{(\text{syn})} + Q_\gamma^{(\text{ics})} + \mathcal{L}_\gamma^{(\gamma\gamma)} + \mathcal{L}_\gamma^{(\text{ssa})} \quad (10)$$

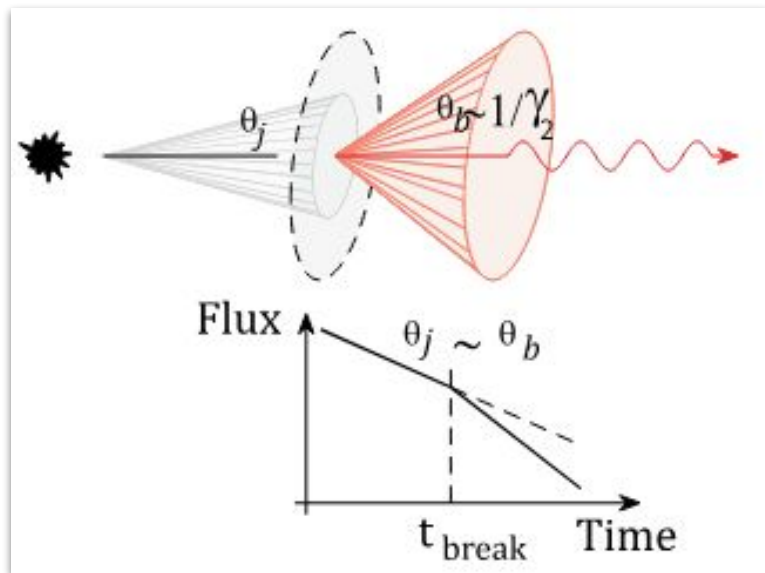


Thermal + Non-thermal electron distribution

(Giannios & Spitkovsky 2009, Warren et al. 2022)



Relativistic beaming - Jet breaks



Relativistically moving plasma with $\Gamma \gg 1$ emits radiation within a cone of half opening-angle:

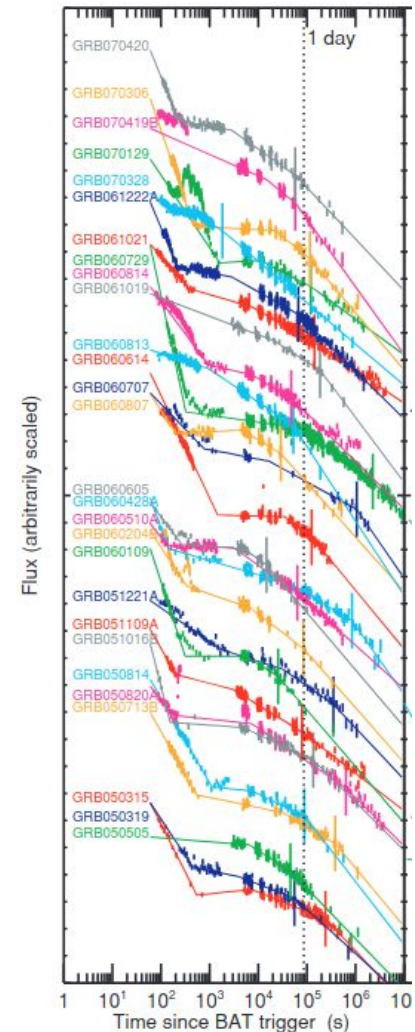
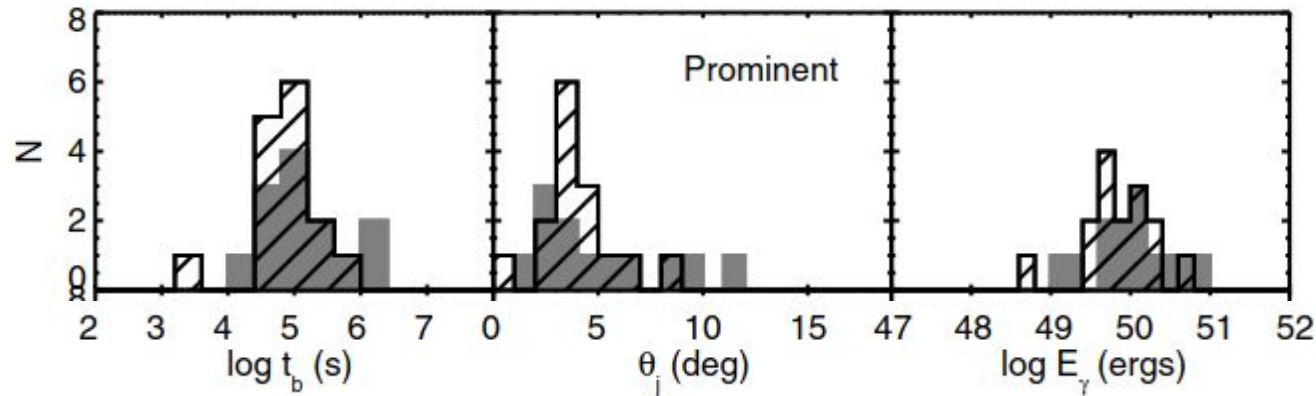
$$\theta_b \sim \frac{1}{\Gamma} \sim \frac{0.29 \text{ deg}}{\Gamma_2}$$

Beaming angle > jet opening angle $\rightarrow$ rapid decrease in flux (**jet break**)

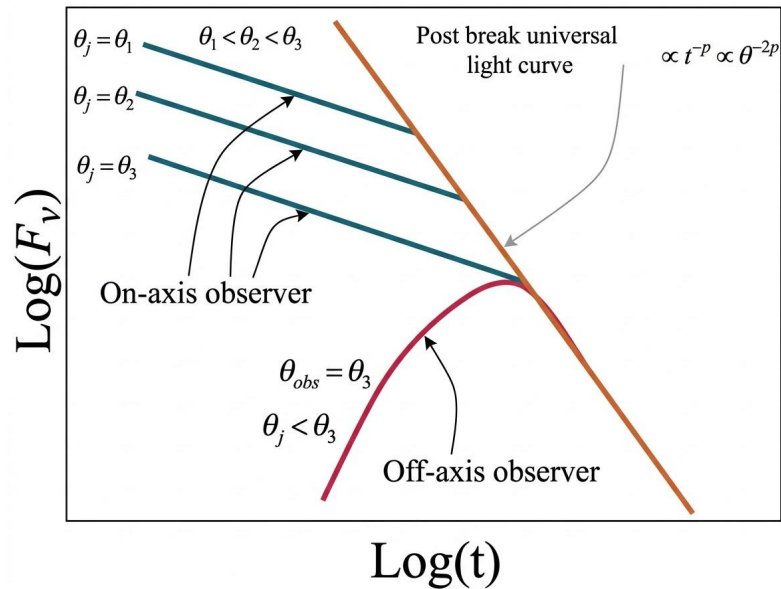
$$\theta_j = 0.057 \left(\frac{t_j}{1 \text{ day}} \right)^{3/8} \left(\frac{1+z}{2} \right)^{-3/8} \left[\frac{E_{\text{iso}}(\gamma)}{10^{53} \text{ ergs}} \right]^{-1/8} \\ \times \left(\frac{\eta_\gamma}{0.2} \right)^{1/8} \left(\frac{n}{0.1 \text{ cm}^{-3}} \right)^{1/8},$$

GRB jet breaks

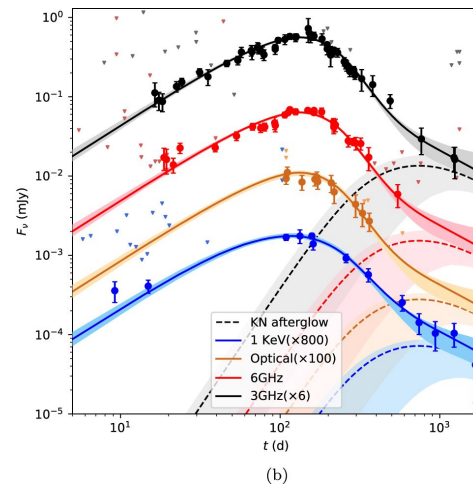
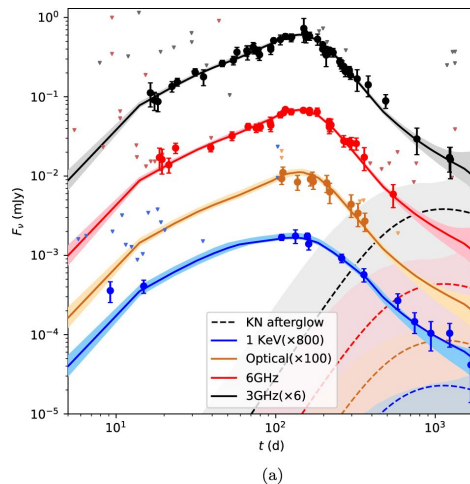
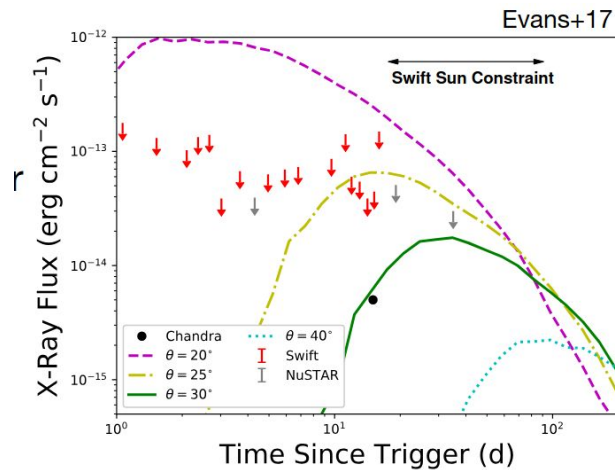
- GRB jets are very well collimated outflows !
- Geometrical beaming is important $f_b = \left(\frac{1 - \cos \theta_b}{2} \right) \xrightarrow{\theta_b \ll 1} \frac{\theta_b^2}{2}$
- Reduced true energetics $E_\gamma = f_b E_{\gamma, iso} = \frac{\theta_b^2}{2} E_{\gamma, iso}$



Off-axis GRB afterglows

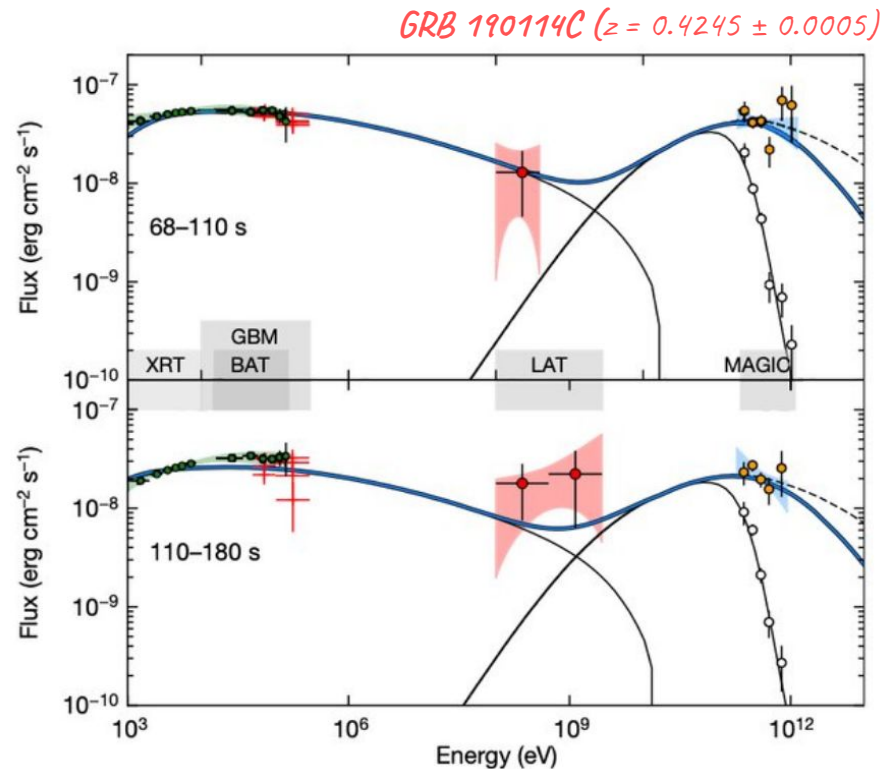
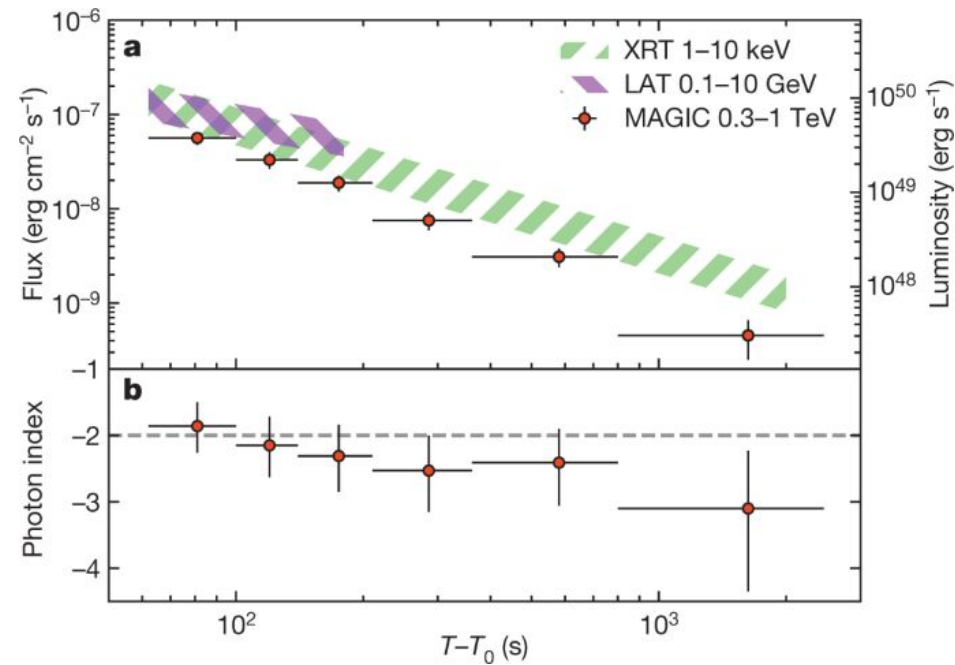


GRB 170817A ($z = 0.099$)



Wang et al. 2023, ApJ

GRBs detected at VHE energies



MAGIC Collaboration 2019, Nature

Open questions & Outlook

Part 1: Prompt emission

1. What causes the observed variability?
2. Are GRB jets magnetic or kinetic dominated flows?
3. What is the baryonic loading (protons/neutrons) of the jet?
4. How are particles accelerated?
5. What produces low-energy spectral breaks in GRB spectra?



Part 2: Afterglow emission

1. What produces flares and plateaus in X-ray afterglows ?
2. What are the expected ϵ_B , ϵ_e parameters for relativistic shocks?
3. Do the shock microphysical parameters evolve with time?
4. How does the pair loading affect the afterglow emission?

Outlook: TeV prompt emission, γ -ray polarization, neutrinos + GWs ??

Useful References



1. [Ruderman 1975, AAS](#)
2. [Cavallo & Rees 1997, MNRAS](#)
3. [Goodman 1986, ApJL](#)
4. [Paczynski 1986, ApJL](#)
5. [Burgess et al. 2020, Nature Astronomy](#)
6. [Abbott et al. 2017, ApJ](#)
7. [Troja et al 2017, Nature](#)
8. [Piran 2004, Review of Modern Physics](#) (theoretical review)
9. [Vigliano & Longo 2024, Universe](#) (recent review on observations)
10. Blandford & McKee 1976, Phys. Fluids
11. [Sari, Piran, Narayan 1998, ApJL](#)
12. Chiang & Dermer 1999, ApJ
13. [Miceli & Nava 2022, Galaxies](#) (recent review)

Part 4: AfterglowPy



<https://github.com/geoffryan/afterglowpy>

<https://afterglowpy.readthedocs.io/en/stable/quickstart.html>

AfterglowPy: Installation

<https://afterglowpy.readthedocs.io/en/stable/quickstart.html>

<https://github.com/geoffryan/afterglowpy>

Installation/Building

afterglowpy is available via `pip` :

```
$ pip install afterglowpy
```



afterglowpy is compatible with Numpy v1 and v2, Python 3.8+, and runs on MacOS, Linux, and Windows.

If you are working on a local copy of this repo and would like to install from source, you can the run the following from the top level directory of the project.

```
$ pip install -e .
```



[Ryan et al. 2020 , ApJ](#)

AfterglowPy: Numerical GRB Afterglow Models

<https://afterglowpy.readthedocs.io/en/stable/quickstart.html>

<https://github.com/geoffryan/afterglowpy>

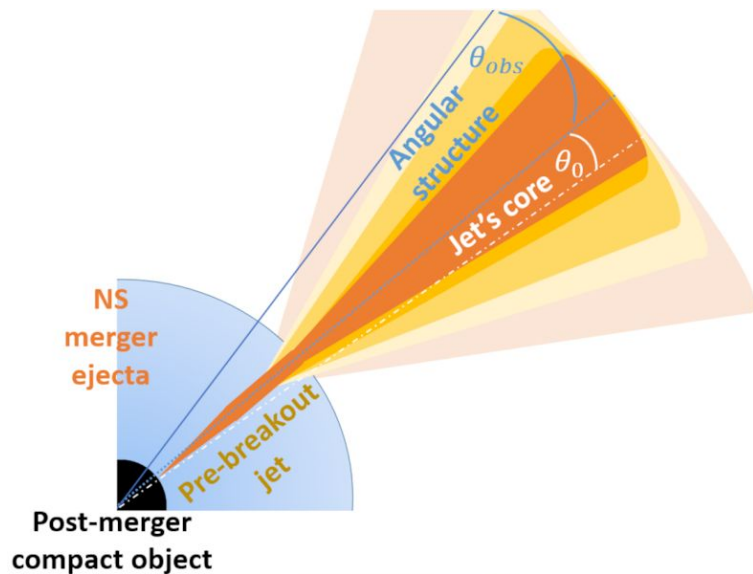
Features

afterglowpy computes synchrotron emission from the forward shock of a relativistic blast wave. It includes:

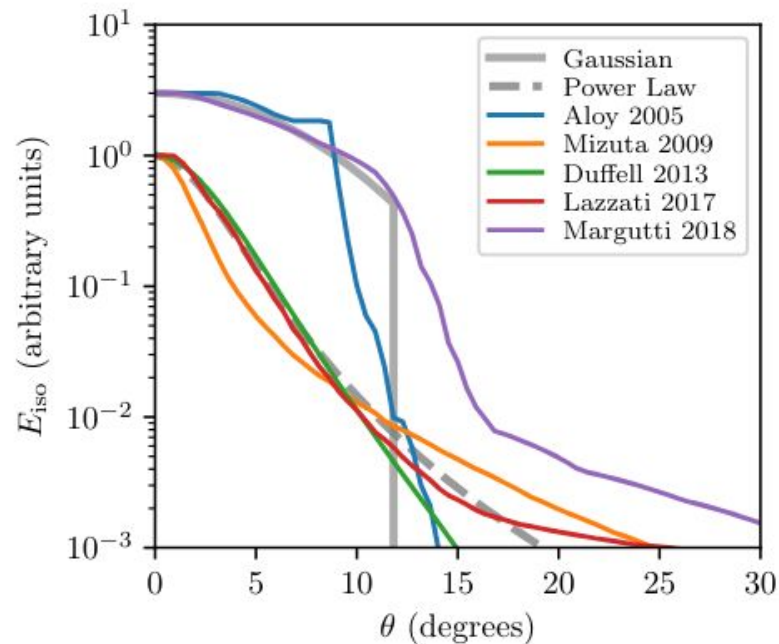
- Fully trans-relativistic shock evolution through a constant density medium.
- On-the-fly integration over the equal-observer-time slices of the shock surface.
- Approximate prescription for jet spreading.
- Arbitrary viewing angles.
- Angularly structured jets, ie. $E(\theta)$
- Spherical velocity-stratified outflows, ie. $E(u)$
- Counter-jet emission.
- Deep Newtonian emission.
- Image moments suitable for astrometry: centroid position and image size.

[Ryan et al. 2020 , ApJ](#)

Afterglow light curves from structured jets

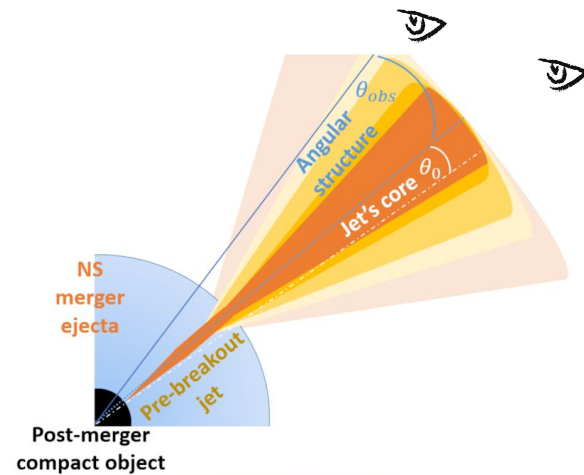
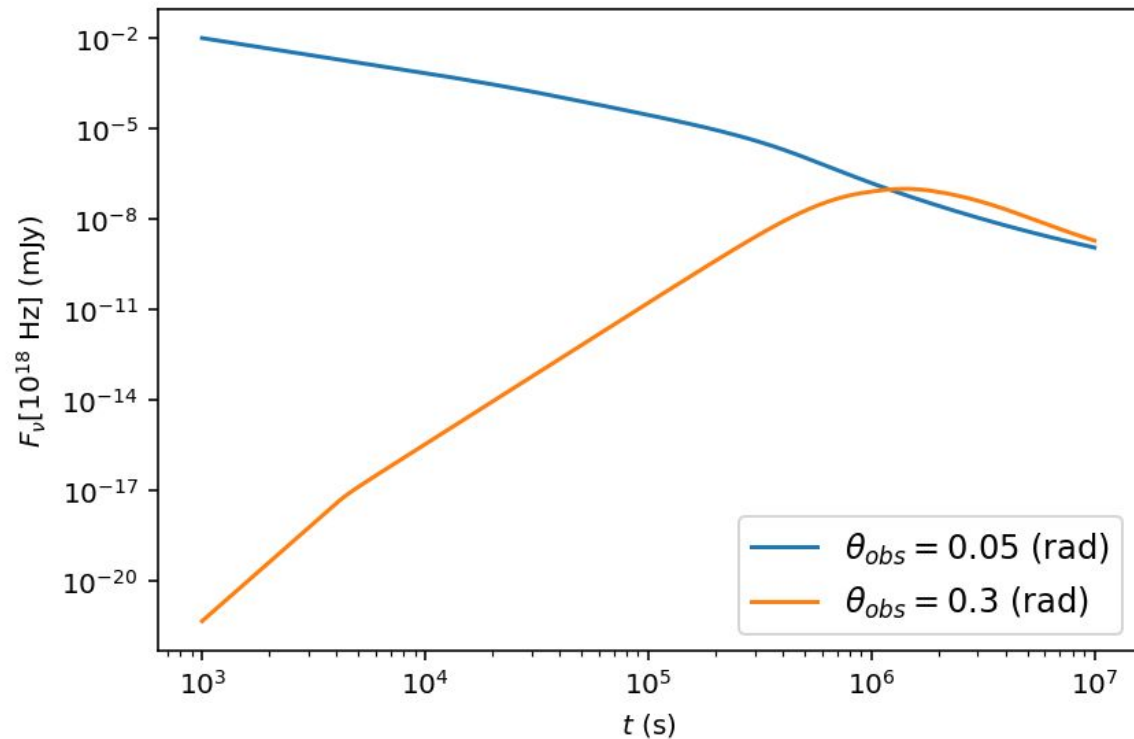


[Beniamini et al. 2019, ApJ](#)

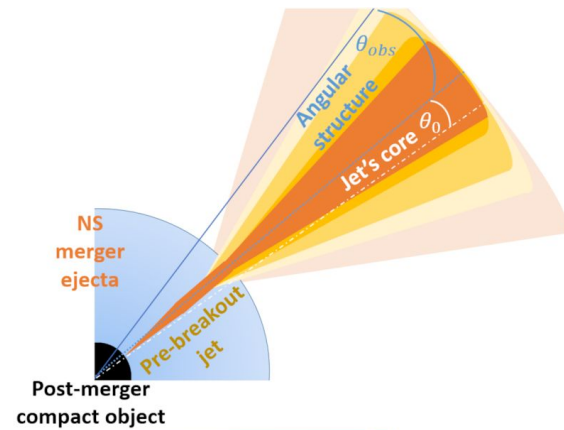
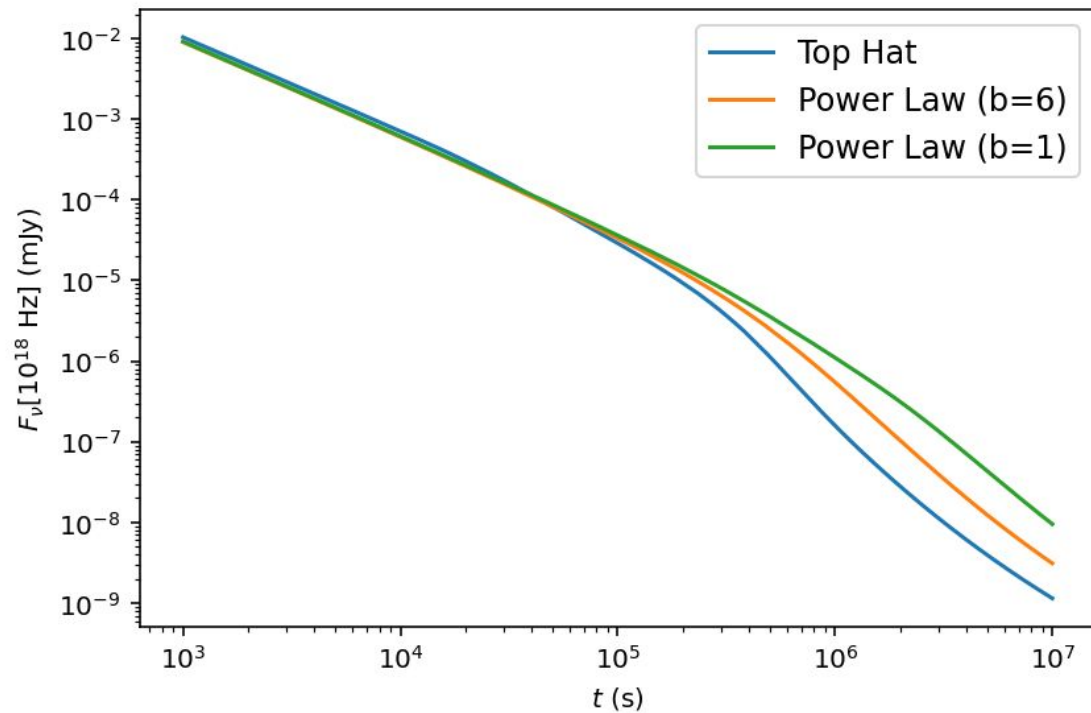


[Ryan et al. 2020, ApJ](#)

Example 1: On axis vs. Off axis observer



Example 2: Top-Hat vs. Power-Law

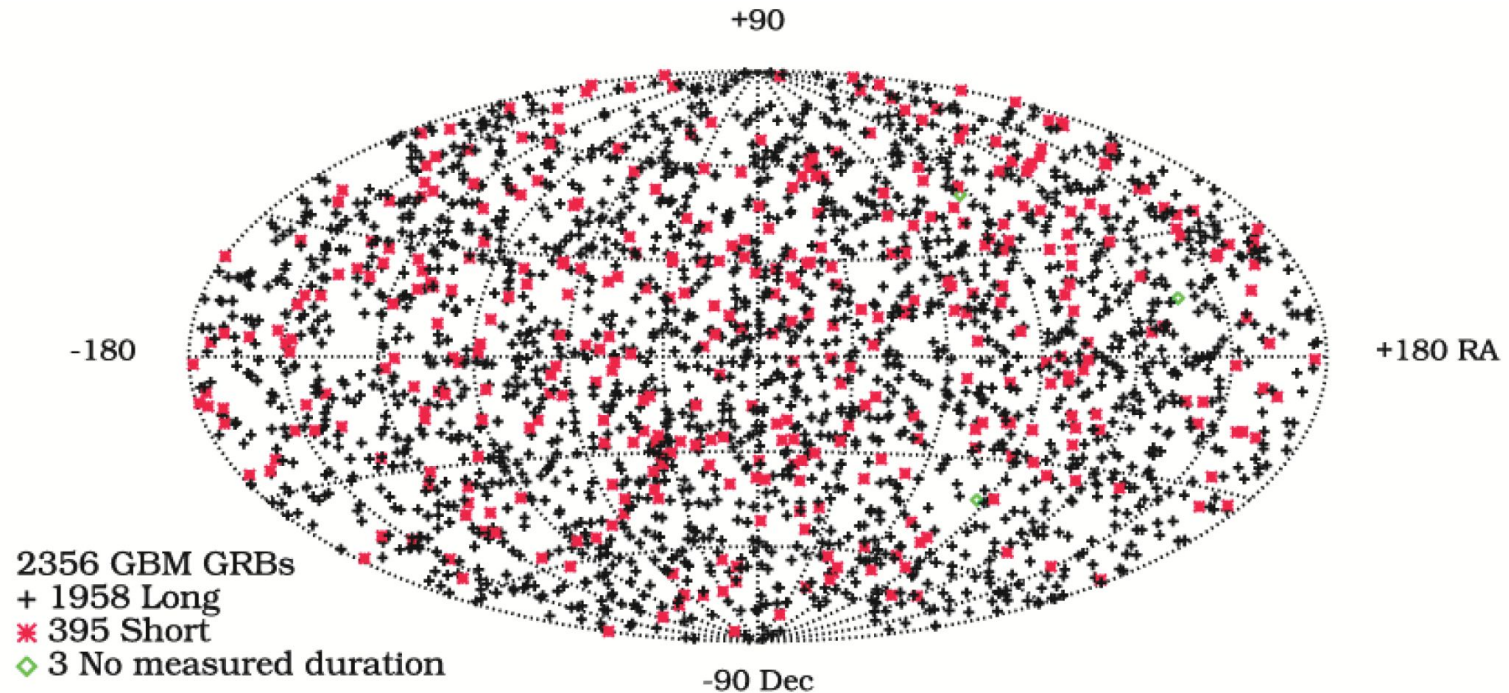


Backup slides

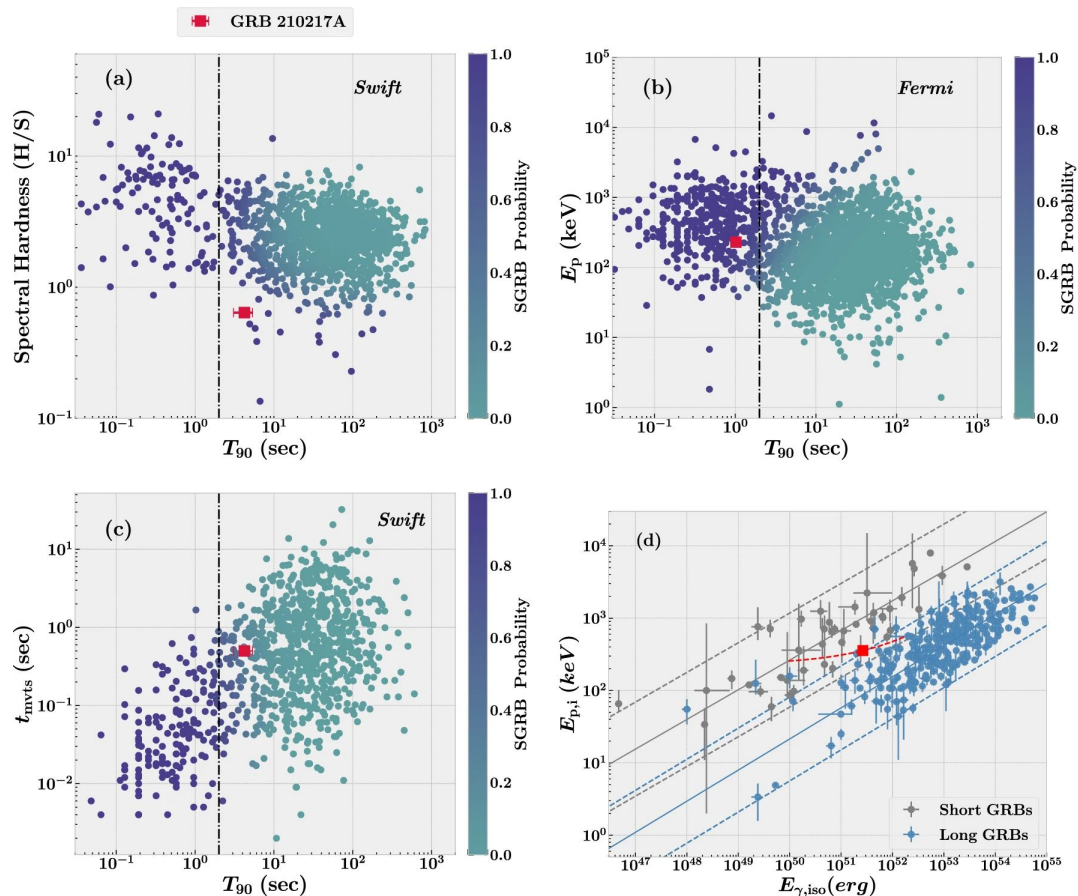


The Fermi era (2008 - today)

2356 bursts



GRB observations with modern observatories



- Similar distributions with BATSE
- Variability is shorter for short GRBs
- Spectral peak energy correlates with total γ -ray energy
- No common explanation for all these trends !

[Dimple et al. 2022, J Astrophys Astron 43, 39](#)

GRB redshift distribution

